

$$1 \{1, 0, 0\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{a_0}}}{\sqrt{\pi}}$$

$$2 \{2, 0, 0\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{2a_0}} \left(\frac{r}{a_0} - 2\right)}{4 \sqrt{2\pi}}$$

$$3 \{2, 1, -1\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{2a_0} - i\phi} r \sin(\theta)}{8 a_0 \sqrt{\pi}}$$

$$4 \{2, 1, 0\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{2a_0}} r \cos(\theta)}{4 a_0 \sqrt{2\pi}}$$

$$5 \{2, 1, 1\} \frac{\sqrt{\frac{1}{a_0^3}} e^{i\phi - \frac{r}{2a_0}} r \sin(\theta)}{8 a_0 \sqrt{\pi}}$$

$$6 \{3, 0, 0\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{3a_0}} \left(\frac{4r^2}{9a_0^2} - \frac{4r}{a_0} + 6\right)}{18 \sqrt{3\pi}}$$

$$7 \{3, 1, -1\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{3a_0} - i\phi} r \left(\frac{2r}{3a_0} - 4\right) \sin(\theta)}{54 a_0 \sqrt{\pi}}$$

$$8 \{3, 1, 0\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{3a_0}} r \left(\frac{2r}{3a_0} - 4\right) \cos(\theta)}{27 a_0 \sqrt{2\pi}}$$

$$9 \{3, 1, 1\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{i\phi - \frac{r}{3a_0}} r \left(\frac{2r}{3a_0} - 4\right) \sin(\theta)}{54 a_0 \sqrt{\pi}}$$

$$10 \quad \{3, 2, -2\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{3a_0} - 2i\phi} r^2 \sin^2(\theta)}{162 a_0^2 \sqrt{\pi}}$$

$$11 \quad \{3, 2, -1\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{3a_0} - i\phi} r^2 \sin(2\theta)}{162 a_0^2 \sqrt{\pi}}$$

$$12 \quad \{3, 2, 0\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{3a_0}} r^2 (3 \cos(2\theta) + 1)}{162 a_0^2 \sqrt{6\pi}}$$

$$13 \quad \{3, 2, 1\} \frac{\sqrt{\frac{1}{a_0^3}} e^{i\phi - \frac{r}{3a_0}} r^2 \sin(2\theta)}{162 a_0^2 \sqrt{\pi}}$$

$$14 \quad \{3, 2, 2\} \frac{\sqrt{\frac{1}{a_0^3}} e^{2i\phi - \frac{r}{3a_0}} r^2 \sin^2(\theta)}{162 a_0^2 \sqrt{\pi}}$$

$$15 \quad \{4, 0, 0\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{4a_0}} \left(\frac{r^3}{8a_0^3} - \frac{3r^2}{a_0^2} + \frac{18r}{a_0} - 24 \right)}{192 \sqrt{\pi}}$$

$$16 \quad \{4, 1, -1\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{4a_0} - i\phi} r \left(\frac{r^2}{4a_0^2} - \frac{5r}{a_0} + 20 \right) \sin(\theta)}{128 a_0 \sqrt{10\pi}}$$

$$17 \quad \{4, 1, 0\} \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{4a_0}} r \left(\frac{r^2}{4a_0^2} - \frac{5r}{a_0} + 20 \right) \cos(\theta)}{128 a_0 \sqrt{5\pi}}$$

$$18 \quad \{4, 1, 1\} \frac{\sqrt{\frac{1}{a_0^3}} e^{i\phi - \frac{r}{4a_0}} r \left(\frac{r^2}{4a_0^2} - \frac{5r}{a_0} + 20 \right) \sin(\theta)}{128 a_0 \sqrt{10\pi}}$$

$$19 \{4, 2, -2\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{4a_0} - 2i\phi} r^2 \left(\frac{r}{2a_0} - 6\right) \sin^2(\theta)}{512 a_0^2 \sqrt{6\pi}}$$

$$20 \{4, 2, -1\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{4a_0} - i\phi} r^2 \left(\frac{r}{2a_0} - 6\right) \cos(\theta) \sin(\theta)}{256 a_0^2 \sqrt{6\pi}}$$

$$21 \{4, 2, 0\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{-\frac{r}{4a_0}} r^2 \left(\frac{r}{2a_0} - 6\right) (3 \cos(2\theta) + 1)}{3072 a_0^2 \sqrt{\pi}}$$

$$22 \{4, 2, 1\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{i\phi - \frac{r}{4a_0}} r^2 \left(\frac{r}{2a_0} - 6\right) \cos(\theta) \sin(\theta)}{256 a_0^2 \sqrt{6\pi}}$$

$$23 \{4, 2, 2\} - \frac{\sqrt{\frac{1}{a_0^3}} e^{2i\phi - \frac{r}{4a_0}} r^2 \left(\frac{r}{2a_0} - 6\right) \sin^2(\theta)}{512 a_0^2 \sqrt{6\pi}}$$

$$24 \{4, 3, -3\} - \frac{\left(\frac{1}{a_0^3}\right)^{3/2} e^{-\frac{r}{4a_0} - 3i\phi} r^3 \sin^3(\theta)}{6144 \sqrt{\pi}}$$

$$25 \{4, 3, -2\} - \frac{\left(\frac{1}{a_0^3}\right)^{3/2} e^{-\frac{r}{4a_0} - 2i\phi} r^3 \cos(\theta) \sin^2(\theta)}{1024 \sqrt{6\pi}}$$

$$26 \{4, 3, -1\} - \frac{\left(\frac{1}{a_0^3}\right)^{3/2} e^{-\frac{r}{4a_0} - i\phi} r^3 (5 \cos(2\theta) + 3) \sin(\theta)}{4096 \sqrt{15\pi}}$$

$$27 \{4, 3, 0\} - \frac{\left(\frac{1}{a_0^3}\right)^{3/2} e^{-\frac{r}{4a_0}} r^3 \cos(\theta) (5 \cos(2\theta) - 1)}{6144 \sqrt{5\pi}}$$

$$28 \{4, 3, 1\} \frac{\left(\frac{1}{a_0^3}\right)^{3/2} e^{i\phi - \frac{r}{4a_0}} r^3 (5 \cos(2\theta) + 3) \sin(\theta)}{4096 \sqrt{15\pi}}$$

$$29 \{4, 3, 2\} \frac{\left(\frac{1}{a_0^3}\right)^{3/2} e^{2i\phi - \frac{r}{4a_0}} r^3 \cos(\theta) \sin^2(\theta)}{1024 \sqrt{6\pi}}$$

$$30 \{4, 3, 3\} \frac{\left(\frac{1}{a_0^3}\right)^{3/2} e^{3i\phi - \frac{r}{4a_0}} r^3 \sin^3(\theta)}{6144 \sqrt{\pi}}$$