

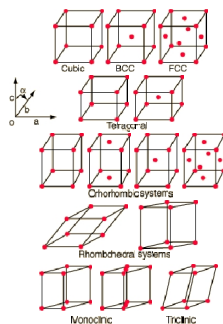
## Fizičko-hemijski aspekti nauke o materijalima

Deo 1  
Igor Pašti

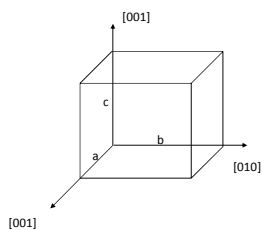
### Sadržaj 1.1.

- Struktura kristala
- Elektronska struktura čvrstih materijala

#### 7 sistema 14 Bravaisovih rešetki



### Milerovi indeksi (hkl):



Pravci:  $[hkl]$   
 Porodice pravaca:  $\langle hkl \rangle$   
 Ravnj:  $\{hkl\}$   
 Porodice ravnj:  $\{hkl\}$

Da bi se identifikovale ravnj:

Korak 1 : identifikovati preseke na x-, y- i z- osama.

Korak 2 : Odrediti preseke u frakcionim koordinatama

Korak 3 : Uzeti recipročne vrednosti frakcionih koordinata odsečaka

### Milerovi indeksi(hkl):

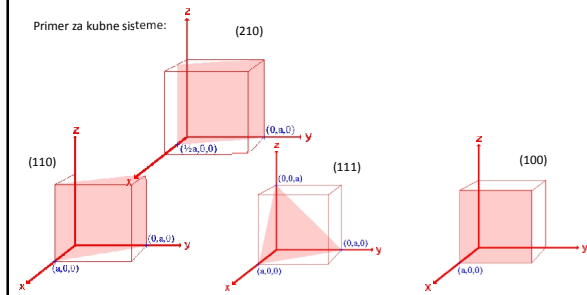
Da bi se identifikovale ravnj:

Korak 1 : identifikovati preseke na x-, y- i z- osama.

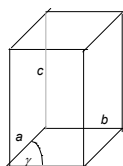
Korak 2 : Odrediti preseke u frakcionim koordinatama

Korak 3 : Uzeti recipročne vrednosti frakcionih koordinata odsečaka

Primer za kubne sisteme:



### Hexagonalni sistemi



$$a = b, c$$

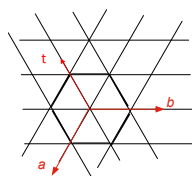
$$\angle = 120^\circ$$

4 indeksa (Weberovi simboli)

$(a \ b \ t \ c)$

$$a + b + t = 0$$

label 'low-index' planes parallel to c axis:



## Periodni sistem

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| H  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    | He |
| Li | Be |    |    |    |    |    |    |    |    |    |    | B  | C  | N  | O  | F  | Ne |
| Na | Mg |    |    |    |    |    |    |    |    |    |    | Al | Si | P  | S  | Cl | Ar |
| K  | Ca | Sc | Ti | V  | Cr | Mn | Fe | Co | Ni | Cu | Zn | Ga | Ge | As | Se | Br | Kr |
| Rb | Sr | Y  | Zr | Nb | Mo | Tc | Ru | Rh | Pd | Ag | Cd | In | Sn | Sb | Te | I  | Xe |
| Cs | Ba | La | Hf | Ta | W  | Re | Os | Ir | Pt | Au | Hg | Tl | Pb | Bi | Po | At | Rn |
| Fr | Ra | Ac |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |

FCC
  BCC
  HCP
  Diamond
  Other

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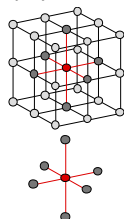
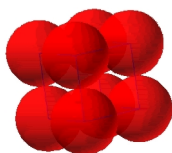
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### Jednostavna kubna struktura Simple Cubic Structure (SC)

- Retka zbog male gustine pakovanja (samo Po ima ovu strukturu)
- Pravci gustog pakovanja su ivice kocke.
  - koordinacioni # = 6  
(# broj najbližih suseda)



Broj atoma u ćeliji?

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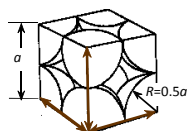
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Faktor pakovanja atoma  
Atomic Packing Factor (APF)

$$\text{APF} = \frac{\text{Zapremina atom u jediničnoj ćeliji}^*}{\text{Zapremina jedinične ćelije}}$$

\*pretpostavlja čvrste sfere

- APF za SCC= 0.52



Pravci gustog pakovanja

sadrži  $8 \times \frac{1}{8} =$

1 atom/jedinična ćelija

The diagram illustrates the calculation of the Atomic Packing Factor (APF) for a unit cell. It shows a unit cell (Jedinična ćelija) with a green vertical bar representing an atom (Atom) and an orange square representing the unit cell volume (zapremina). The unit cell is divided into four smaller squares, each with a side length of  $0.5a$ . The unit cell volume is calculated as  $a^3$ . The atomic volume is represented by a blue square with side length  $a$ . The APF is calculated as the ratio of the atomic volume to the unit cell volume.

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### APF za BCC

- APF = 0.68

Koordinacioni broj?

Pravci gustog pakovanja su dijagonale kocke:  
Dužina =  $4R = \sqrt{3}a$

atoma  
Jedinična ćelija →  $2 \cdot \frac{4}{3} \pi \left( \frac{\sqrt{3}a}{4} \right)^3$  ← zapremina  
atom  
APF =  $\frac{\text{zapremina atoma}}{\text{zapremina Jedinična ćelija}} = \frac{2 \cdot \frac{4}{3} \pi \left( \frac{\sqrt{3}a}{4} \right)^3}{a^3}$

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### Površinski centrirana kubna rešetka (FCC)

- Atomi se dodiruju duž dijagonala strana kocke.

Al, Cu, Au, Pb, Ni, Pt, Ag      • Koordinacioni # = 12

4 atoma/jedinična ćelija: 6 strana x 1/2 + 8 ćoškovni x 1/8

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### APF za FCC

- APF za FCC = 0.74

Maksimalni APF!

Pravci gustog pakovanja:  
Dužina =  $4R = \sqrt{2}a$

4 atoms/unit cell

atoma  
Jedinična ćelija →  $4 \cdot \frac{4}{3} \pi \left( \frac{\sqrt{2}a}{4} \right)^3$  ← zapremina  
atom  
APF =  $\frac{\text{zapremina atoma}}{\text{zapremina Jedinična ćelija}} = \frac{4 \cdot \frac{4}{3} \pi \left( \frac{\sqrt{2}a}{4} \right)^3}{a^3}$

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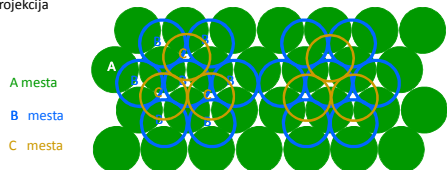
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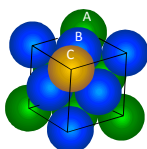
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## FCC slaganje

- ABCABC... Sekvenca duž 111 pravca
- 2D projekcija

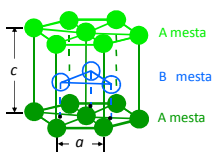


- jednična ćelija

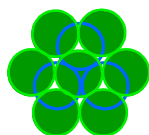


## Heksagonalna gusto pakovanje (HCP)

- ABAB... sekvenca
- 3D projekcija



- 2D projekcija



- koordinacioni # = 12

- APF = 0.74

- $c/a = 1.633$

6 atoma/jediničnoj ćeliji

Na primer: Cd, Mg, Ti, Zn

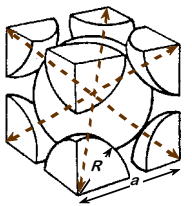
Teorijska gustina,  $\rho$ 

$$\text{Gustina} = \rho = \frac{\text{Masa atoma u jediničnoj ćeliji}}{\text{Zapremina jedinične ćelije}}$$

$$\rho = \frac{nA}{V_c N_A}$$

$n$  = broj atoma u jediničnoj ćeliji  
 $A$  = atomska težina  
 $V_c$  = zapremina jedinične ćelije =  $a^3$  za kubne sisteme  
 $N_A$  = Avogadrov broj  
 $= 6.022 \times 10^{23}$  atom/mol

### Teorijska gustina, $\rho$



Primer: Cr (BCC)

$A = 52.00 \text{ g/mol}$

$R = 0.125 \text{ nm}$

$n = 2 \text{ atoma u jediničnoj ćeliji}$

$a = 4R / \sqrt{3} = 0.2887 \text{ nm}$

atoma  
Jedinična ćelija 2 52.00

$\rho = \frac{g}{\text{mol}}$

$\rho = \frac{2 \times 52.00 \text{ g/mol}}{(0.2887 \text{ nm})^3 \times 10^{21} \text{ cm}^3/\text{nm}^3} = 7.18 \text{ g/cm}^3$

$\rho_{\text{teorijska}} = 7.18 \text{ g/cm}^3$

$\rho_{\text{stvarna}} = 7.19 \text{ g/cm}^3$

zapremina  
Jedinična ćelija

atom  
mol

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### Gustine različitih klasa materijala

Uopšteno

$\rho_{\text{metali}} > \rho_{\text{keramike}} > \rho_{\text{polimeri}}$

Zašto?

**Metali imaju:**

- gusto pakovanje (metalna veza)
- često velike atomske mase

**Keramike imaju...**

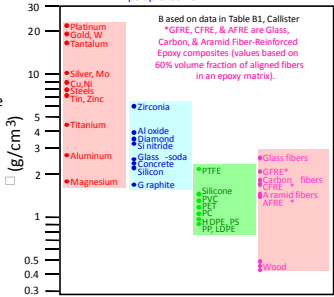
- manje gusta pakovanja
- lakše elemente

**Polimeri imaju...**

- malu gustinu pakovanja (često amorfni)
- lake elemente (C, H, O)

**Kompoziti imaju...**

- nešto između



Based on data in Table B.1, Callister

\*GFR, CFR, & AFR are Glass, Carbon, & Aramid Fiber-Reinforced Epoxy composites (values based on 60% volume fraction of aligned fibers in an epoxy matrix).

Data from Table B.1, Callister & Rethwisch, 8e.

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### Elektronska struktura čvrstih metala

- Zonska teorija
- Elektronski provodnici: uglavnom metali
- Izolatori: uglavnom nemetalni materijali
- Poluprovodnici (metaloide)

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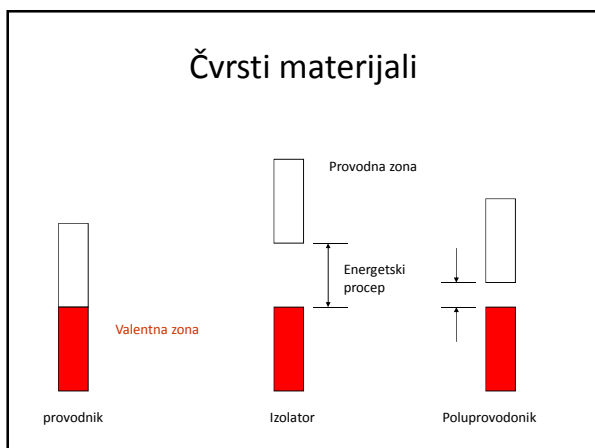
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## Čvrsti materijali




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## Vezivanje u metalima

- Niz pozitivnih jona okružen delokalizovanim valentnim elektronima

- Dobri elektronski provodnici zbog mobilnosti delokalizovanih valentnih elektrona
- Dobri toplotni provodnici

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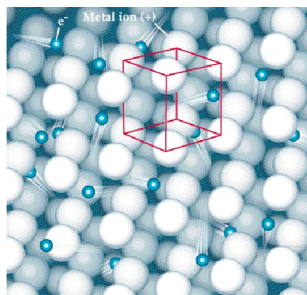
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## Vezivanje u metalima



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## Vezivanje u metalima

- Energetski nivoi formiraju energetske zone ili trake
- Kada se eksitiraju elektroni prelaze na slobodne nivoe u energetskoj zoni
- S obzirom da nema energetskog procepa ovo zahteva vrlo malo energije

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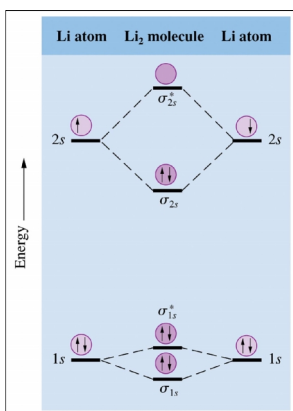
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## Vezivanje u metalima Li prema MO teoriji




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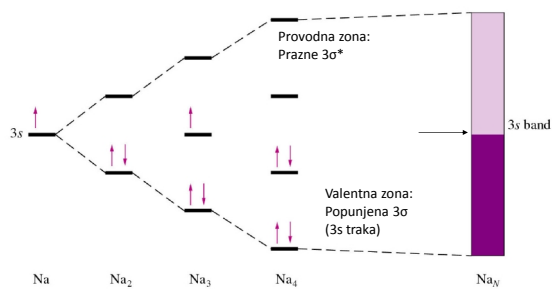
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## Na prema zonskoj teoriji




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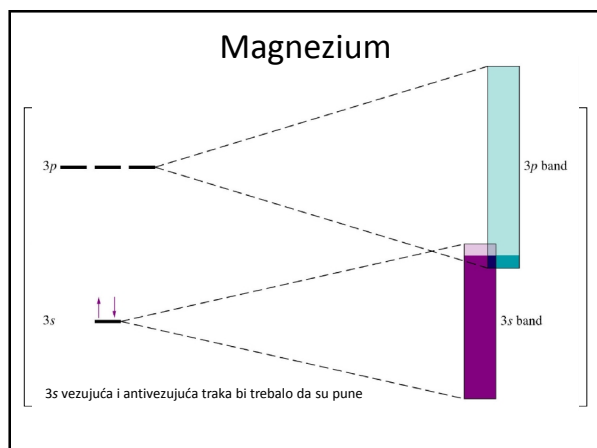
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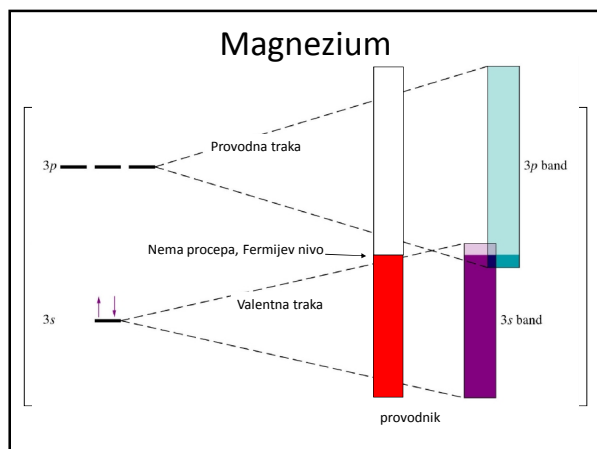
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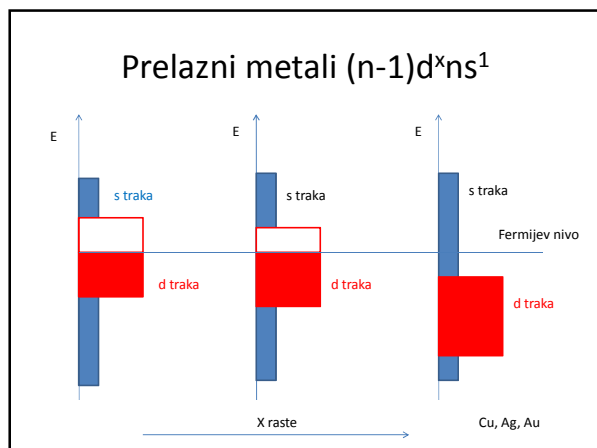
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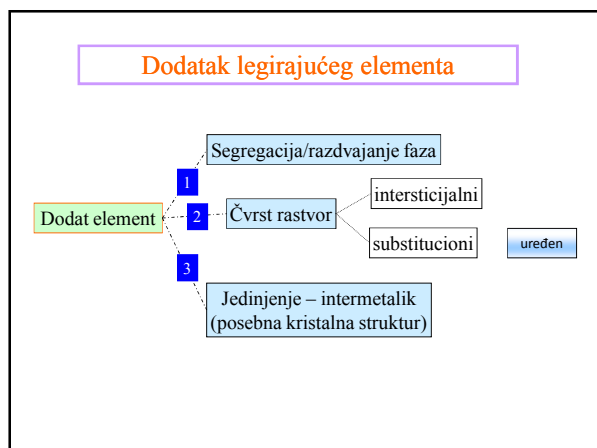
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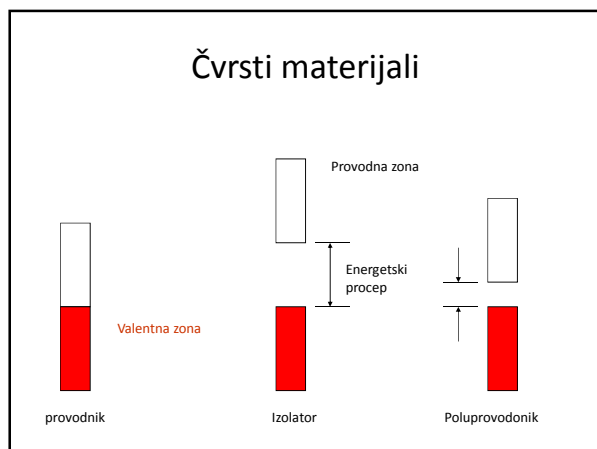
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### Alotropi ugljenika – dijamant vs. grafit

- Dijamant: visoka toplotna provodljivost, ekstremno čvrst, izolator
- Grafit: visoka toplotna provodljivost, provodnik

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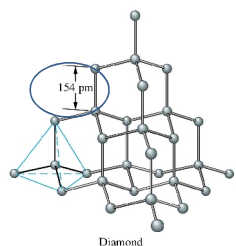
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## Sruktura dijamanta



- **3D struktura, jednostruke veze,  $sp^3$  hibridizacija.**
- **Zašto provodi toplotu?**
  - Kod metala pokretni elektroni nose višak kinetičke energije.
  - Dijamant je izolator bez pokretnih naelektrisanja.
  - Toplota se provodi preko vibracija rešetke
- **4 puta bolji toplotni provodnik od bakra!**

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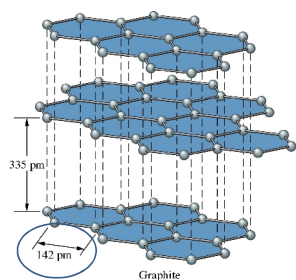
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## Struktura grafita




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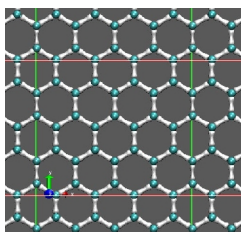
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## Grafit

- **Grafit ima slojevitú strukturu.**
- Grafenski sloj –  $sp^2$  hibridizacija, delokalizovani elektroni, slojevi povezani slabim VdW vezama
- Jedini kovalentni kristal koji provodi struju




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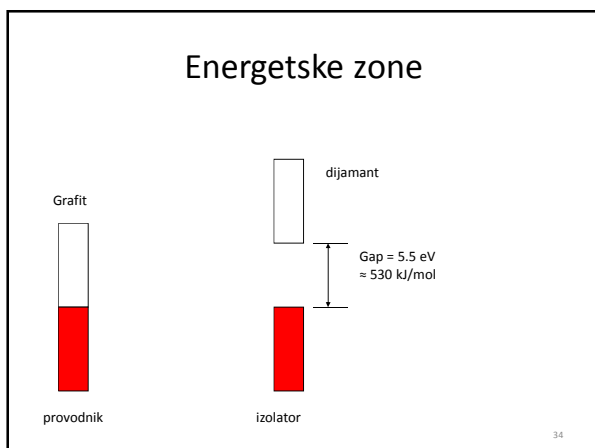
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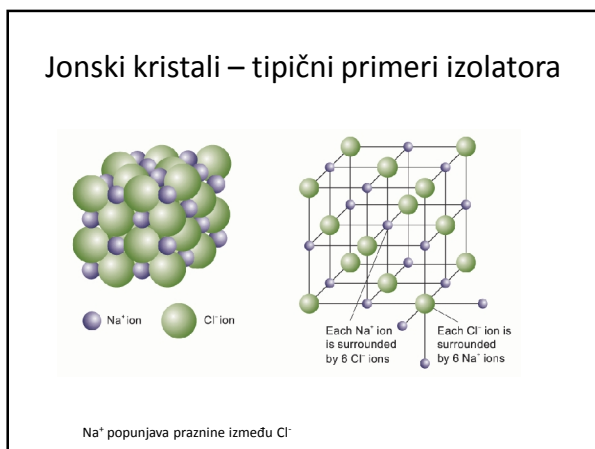
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## Energetske zone

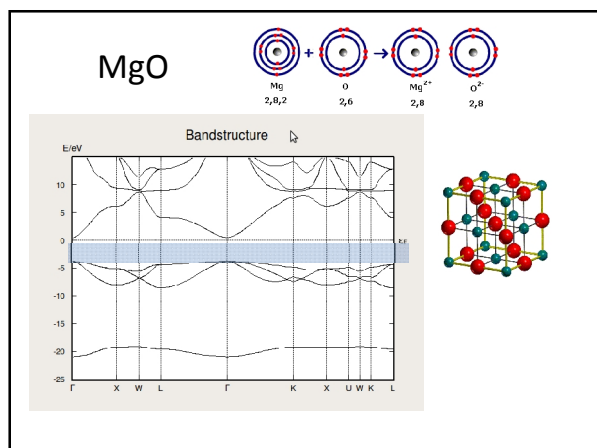


## Jonski kristali – tipični primeri izolatora



| Interstitial site | Tetraedarska                | Oktaedarska                      | Kubna                                   | Kubna                                                              |
|-------------------|-----------------------------|----------------------------------|-----------------------------------------|--------------------------------------------------------------------|
| Coordination      | 4 : 4                       | 6 : 6                            | 8 : 8                                   | 8:4                                                                |
| $r^+/r^-$         | 0.225 – 0.414               | 0.414 – 0.732                    | 0.732 – 1.000                           | 0.732 – 1.000                                                      |
| Examples          | ZnS, most copper(I) halides | Alkali metal halides except CsCl | CsCl, CsBr, CsI, $\text{NH}_4\text{Cl}$ | $\text{CaF}_2$ , $\text{BaF}_2$ , $\text{BaCl}_2$ , $\text{SrF}_2$ |






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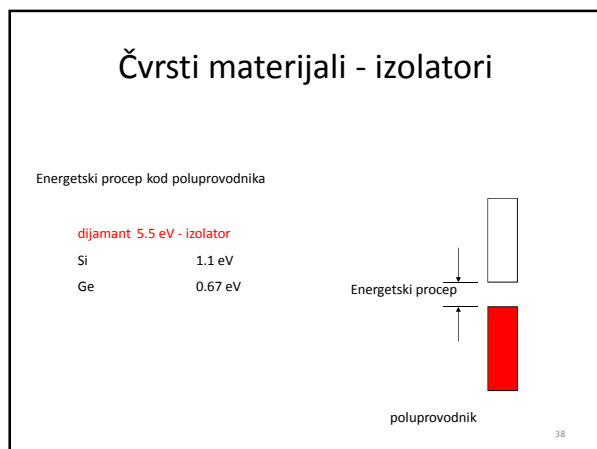
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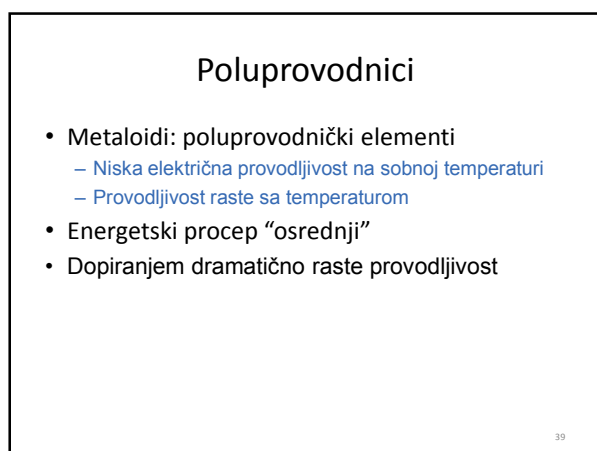
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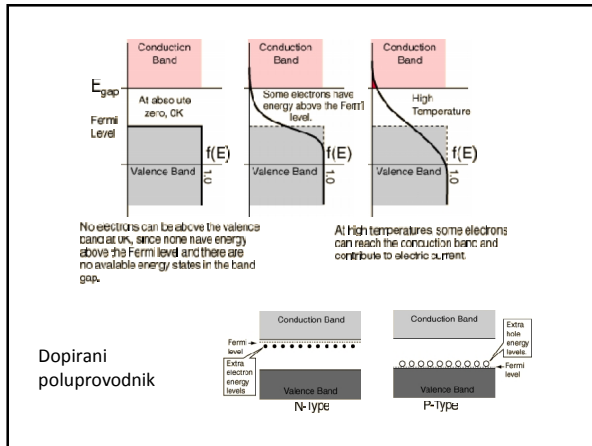
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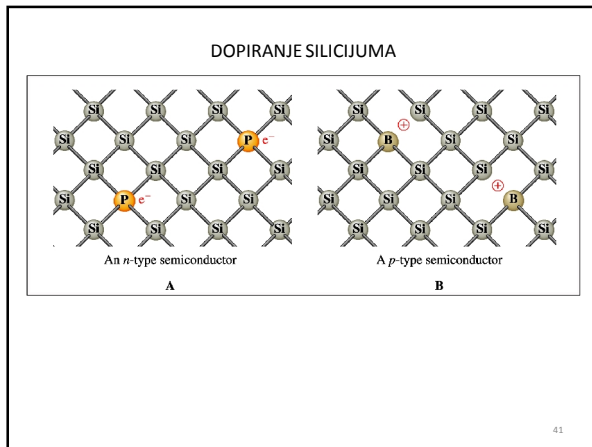
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| 1               | 2               | 3               | 4               | 5               | 6               | 7               | 8               | 9               | 10              | 11              | 12              | 13              | 14              | 15              | 16              | 17              | 18              |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 1<br>H<br>1s    | 2<br>He<br>1s   |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |
| 3<br>Li<br>2s   | 4<br>Be<br>2s   |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |
| 5<br>B<br>2s    | 6<br>C<br>2s    | 7<br>N<br>2s    | 8<br>O<br>2s    | 9<br>F<br>2s    | 10<br>Ne<br>2s  |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |
| 11<br>Na<br>3s  | 12<br>Mg<br>3s  | 13<br>Al<br>3s  | 14<br>Si<br>3s  | 15<br>P<br>3s   | 16<br>S<br>3s   | 17<br>Cl<br>3s  | 18<br>Ar<br>3s  |                 |                 |                 |                 |                 |                 |                 |                 |                 |                 |
| 19<br>K<br>4s   | 20<br>Ca<br>4s  | 21<br>Sc<br>3d  | 22<br>Ti<br>3d  | 23<br>V<br>3d   | 24<br>Cr<br>3d  | 25<br>Mn<br>3d  | 26<br>Fe<br>3d  | 27<br>Co<br>3d  | 28<br>Ni<br>3d  | 29<br>Cu<br>3d  | 30<br>Zn<br>3d  | 31<br>Ga<br>4s  | 32<br>Ge<br>4s  | 33<br>As<br>4s  | 34<br>Se<br>4s  | 35<br>Br<br>4s  | 36<br>Kr<br>4s  |
| 37<br>Rb<br>5s  | 38<br>Sr<br>5s  | 39<br>Y<br>4d   | 40<br>Zr<br>4d  | 41<br>Nb<br>4d  | 42<br>Mo<br>4d  | 43<br>Tc<br>4d  | 44<br>Ru<br>4d  | 45<br>Rh<br>4d  | 46<br>Pd<br>4d  | 47<br>Ag<br>4d  | 48<br>Cd<br>4d  | 49<br>In<br>5s  | 50<br>Sn<br>5s  | 51<br>Sb<br>5s  | 52<br>Te<br>5s  | 53<br>I<br>5s   | 54<br>Xe<br>5s  |
| 55<br>Cs<br>6s  | 56<br>Ba<br>6s  | 57<br>La<br>5d  | 58<br>Ce<br>5d  | 59<br>Pr<br>5d  | 60<br>Nd<br>5d  | 61<br>Pm<br>5d  | 62<br>Sm<br>5d  | 63<br>Eu<br>5d  | 64<br>Gd<br>5d  | 65<br>Tb<br>5d  | 66<br>Dy<br>5d  | 67<br>Ho<br>5d  | 68<br>Er<br>5d  | 69<br>Tm<br>5d  | 70<br>Yb<br>5d  | 71<br>Lu<br>5d  | 72<br>Hf<br>5d  |
| 73<br>Ta<br>5d  | 74<br>W<br>5d   | 75<br>Re<br>5d  | 76<br>Os<br>5d  | 77<br>Ir<br>5d  | 78<br>Pt<br>5d  | 79<br>Au<br>5d  | 80<br>Hg<br>5d  | 81<br>Tl<br>6s  | 82<br>Pb<br>6s  | 83<br>Bi<br>6s  | 84<br>Po<br>6s  | 85<br>At<br>6s  | 86<br>Rn<br>6s  | 87<br>Fr<br>6s  | 88<br>Ra<br>6s  | 89<br>Ac<br>6d  | 90<br>Th<br>6d  |
| 91<br>Pa<br>6d  | 92<br>U<br>6d   | 93<br>Np<br>6d  | 94<br>Pu<br>6d  | 95<br>Am<br>6d  | 96<br>Cm<br>6d  | 97<br>Bk<br>6d  | 98<br>Cf<br>6d  | 99<br>Es<br>6d  | 100<br>Fm<br>6d | 101<br>Md<br>6d | 102<br>No<br>6d | 103<br>Lr<br>6d | 104<br>Rf<br>6d | 105<br>Db<br>6d | 106<br>Sg<br>6d | 107<br>Bh<br>6d | 108<br>Hs<br>6d |
| 109<br>Mt<br>6d | 110<br>Ds<br>6d | 111<br>Rg<br>6d | 112<br>Cn<br>6d | 113<br>Nh<br>7s | 114<br>Fl<br>7s | 115<br>Mc<br>7s | 116<br>Lv<br>7s | 117<br>Ts<br>7s | 118<br>Og<br>7s |                 |                 |                 |                 |                 |                 |                 |                 |

**Groups:**

- Conductors:** Groups 1, 2, 11, 12, 13, 14, 15, 16, 17, 18
- Semiconductors:** Groups 13, 14, 15, 16, 17, 18
- Insulators:** Groups 13, 14, 15, 16, 17, 18

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## Površina

**IDEJA:** Kada se formira površina raspored atoma na površini ostaje sličan kao u kristalu

### SADRŽAJ 1.2.

Čvrsta površina

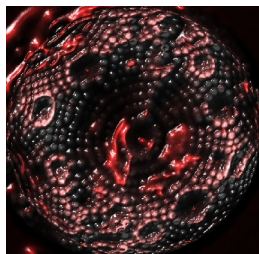
Kristalna struktura

Elektronska struktura

Rekonstrukcija i relaksacija

**Volframova igla**

J. Chem. Phys. 124, 204716 (2006)




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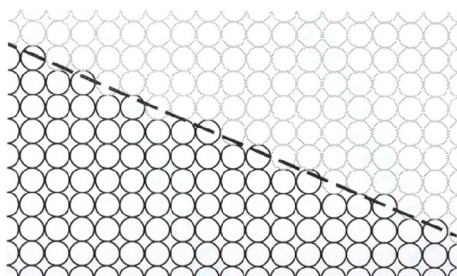
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## Formiranje površine



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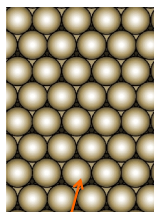
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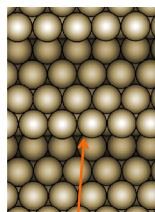
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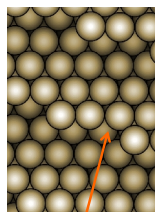
Neke od karakterističnih lokalnih struktura na površinama



Terasa



Stepenik



Kink

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## Notacija površinskih struktura

Ideja:

- Osnovna ponavljajuća jedinica na površini – jedinična ćelija
- Razviti notaciju za opis jedinične ćelije

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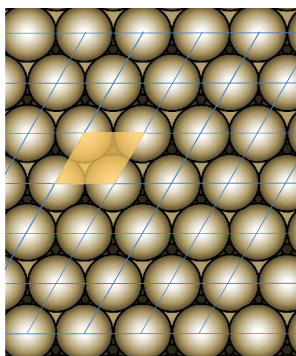
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## Jedinična površinska ćelija



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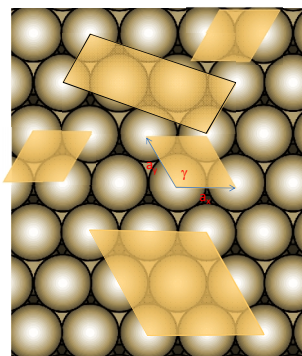
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## Izbor nije jedinstven



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## 2D Bravais rešetke

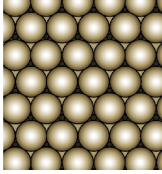
Ideja – klasifikovati jediničnu ćeliju prema simetriji

6 Bravaisovih rešetki u 2D

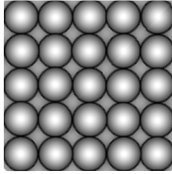
|                     |                                                        | Conventional      | Axes of Conventional                                   |
|---------------------|--------------------------------------------------------|-------------------|--------------------------------------------------------|
| Lattice             | Axes of Primitive Cell                                 | Cell              | Cell                                                   |
| Oblique             | $a_1 \neq a_2, \gamma \neq 90^\circ$ or $120^\circ$    | Parallelogram     | $a_1' \neq a_2', \gamma' \neq 90^\circ$ or $120^\circ$ |
| Centered rectangle  | $a_1 = a_2, \gamma \neq 90^\circ$ or $120^\circ$       | Rectangle         | $a_1' \neq a_2', \gamma' = 90^\circ$                   |
| Primitive rectangle | $a_1 \neq a_2, \gamma = 90^\circ$                      | Rectangle         | $a_1' \neq a_2', \gamma' = 90^\circ$                   |
| Hexagonal           | $a_1 = a_2, \gamma = 120^\circ$<br>with a sixfold axis | Hexagonal         | $a_1' = a_2', \gamma' = 120^\circ$                     |
| Oblique             | $a_1 \neq a_2, \gamma = 120^\circ$                     | Parallelogram     | $a_1' \neq a_2', \gamma' = 120^\circ$                  |
| Square              | $a_1 = a_2$                                            | $90^\circ$ square | $a_1' = a_2', \gamma' = 90^\circ$                      |

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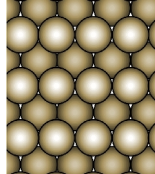
Šestougao



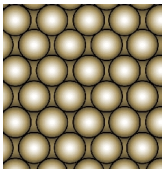
Kvadrat



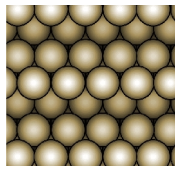
Pravougaonik



Centrirani pravougaonik

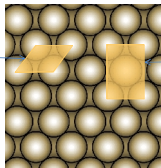


Pravougaonik



## Centrirani pravougaonik

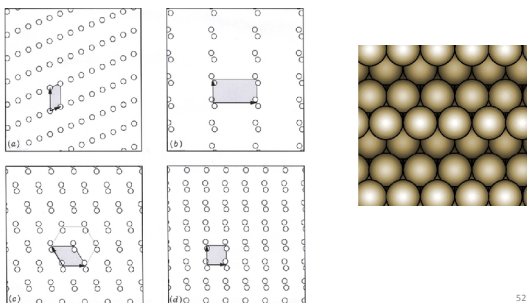
Primitivna  
ćelija



Konvencionalna  
jedinična ćelija

51

## Jedinična ćelija + strukturni motiv



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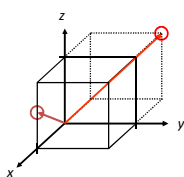
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## Kristalografski pravci



Algoritam

1. Pomeriti vektor da prolazi kroz (0,0,0)
2. Pročitati projekcije u umnošku a, b i c
3. Podesiti na najmanje cele brojeve
4. dati u formi  $[uvw]$

primer:  $1, 0, \frac{1}{2} \Rightarrow 2, 0, 1 \Rightarrow [201]$  $-1, 1, 1 \Rightarrow [\bar{1}11]$  Negativan indeks – crtica iznadFamilija pravaca  $\langle uvw \rangle$ 

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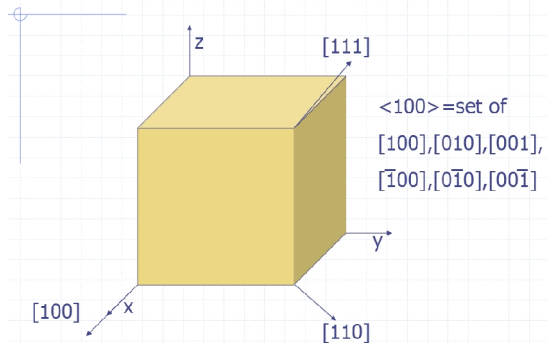
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## Miller indices: Directions




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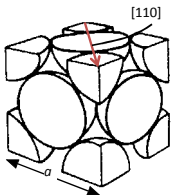
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## Linearna gustina

- Linearna gustina atoma  $\equiv LD = \frac{\text{Broj atoma}}{\text{Jedinica dužine vektora}}$



primer: linearna gustina Al u pravcu [110]

$$a = 0.405 \text{ nm}$$

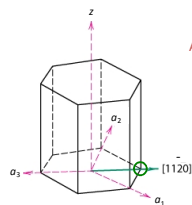
# atoma  $\rightarrow 2$

LD  $\rightarrow \frac{2}{\sqrt{2}a}$

dužina  $\rightarrow \sqrt{2}a$

$3.5 \text{ nm}^{-1}$

## HCP kristalograski pravci

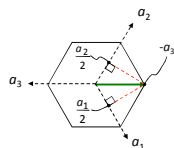


Algoritam

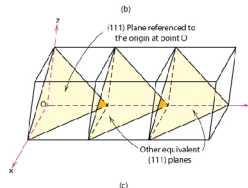
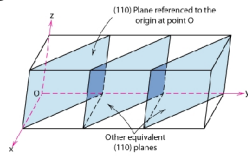
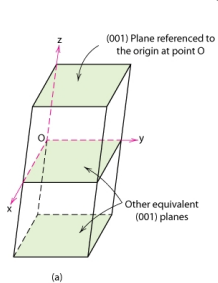
1. Pomeriti vektor da prolazi kroz (0,0,0)
2. Pročitati projekcije u umnošku a, b i c
3. Podesiti na najmanje cele brojeve
4. dati u formi [uvw]

Primer:  $\frac{1}{2}, \frac{1}{2}, -1, 0 \Rightarrow$

$[11\bar{2}0]$



## Kristalogrfske ravni



## Kristalografske ravni

- Milerovi indeksi: kako se određuju?
- Sve paralelne ravni imaju iste Milerove indekse.
- Algoritam
  1. Očitati preseke ravni sa  $a$ ,  $b$ ,  $c$
  2. Uzeti recipročne vrednosti odsečaka
  3. Redukovati na najmanje cele brojeve
  4. U zagrade, bez zareza ( $hkl$ )

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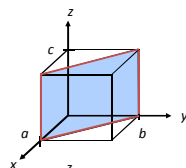
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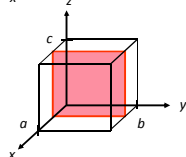
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## Kristalografske ravni

|                     |       |       |            |
|---------------------|-------|-------|------------|
| <u>Primer</u>       | $a$   | $b$   | $c$        |
| 1. Preseci          | 1     | 1     | $\infty$   |
| 2. Recipročno       | $1/1$ | $1/1$ | $1/\infty$ |
| 3. Redukcija        | 1     | 1     | 0          |
| 4. Milerovi indeksi | (110) |       |            |



|                     |         |            |            |
|---------------------|---------|------------|------------|
| <u>Primer</u>       | $a$     | $b$        | $c$        |
| 1. Preseci          | $1/2$   | $\infty$   | $\infty$   |
| 2. Recipročno       | $1/1/2$ | $1/\infty$ | $1/\infty$ |
| 3. Redukcija        | 2       | 0          | 0          |
| 4. Milerovi indeksi | (200)   |            |            |



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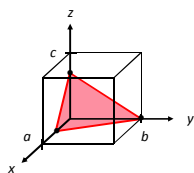
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## Kristalografske ravni

|                     |         |       |         |
|---------------------|---------|-------|---------|
| <u>Primer</u>       | $a$     | $b$   | $c$     |
| 1. Preseci          | $1/2$   | 1     | $3/4$   |
| 2. Recipročno       | $1/1/2$ | $1/1$ | $1/3/4$ |
| 3. Redukcija        | 6       | 3     | 4       |
| 4. Milerovi indeksi | (634)   |       |         |



Porodica ravni  $\{hkl\}$

Primer:  $\{100\} = (100), (010), (001), (\bar{1}00), (01\bar{0}), (00\bar{1})$

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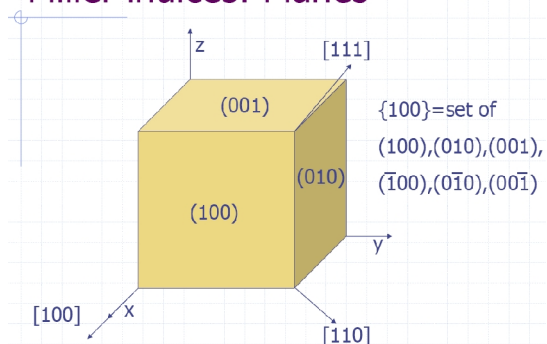
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## Miller indices: Planes




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## Heksagonalni sistem (HCP)

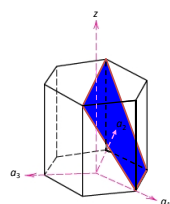
- Ista ideja

Primer

- Preseci
- Recipročno
- Redukcija
- Indeksi

| $a_1$ | $a_2$      | $a_3$ | $c$ |
|-------|------------|-------|-----|
| 1     | $\infty$   | -1    | 1   |
| 1     | $1/\infty$ | -1    | 1   |
| 1     | 0          | -1    | 1   |
| 1     | 0          | -1    | 1   |

$(10\bar{1}1)$




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## Površinska gustina

- Utiče na površinsku energiju
- Stabilnost površine
- Reaktivnost površine

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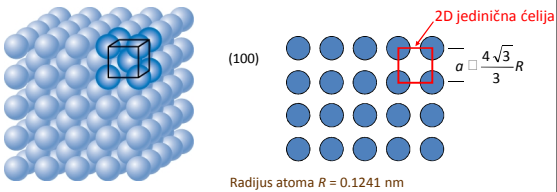
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### Površinska gustina Fe(100)

$T < 912^\circ\text{C}$  BCC struktura.



2D jedinična ćelija

atoma  
2D jed. ćeliji  
1

Površinska gust =  $\frac{1}{a^2} = \frac{1}{\left(\frac{4\sqrt{3}}{3}R\right)^2} = 12.1 \frac{\text{atoma}}{\text{nm}^2} = 1.2 \times 10^{19} \frac{\text{atoma}}{\text{m}^2}$

površina  
2D jed. ćelija

Radius atoma  $R = 0.1241 \text{ nm}$

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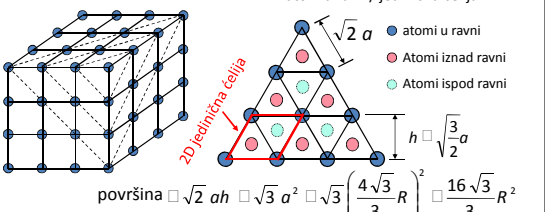
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### Površinska gustina Fe(111)

1 atom u ravni/ jedinična ćelija



2D jedinična ćelija

atomi u ravni  
Atomi iznad ravni  
Atomi ispod ravni

$a \square \sqrt{2} a$   
 $h \square \sqrt{\frac{3}{2}} a$

površina  $\square \sqrt{2} ah \square \sqrt{3} a^2 \square \sqrt{3} \left(\frac{4\sqrt{3}}{3}R\right)^2 \square \frac{16\sqrt{3}}{3} R^2$

atoma  
2D jedinična ćel  
1

Površinska gustina =  $\frac{1}{\frac{16\sqrt{3}}{3} R^2} = 7.0 \frac{\text{atoma}}{\text{nm}^2} = 0.70 \times 10^{19} \frac{\text{atoma}}{\text{m}^2}$

površina  
2D jedinična ćelija

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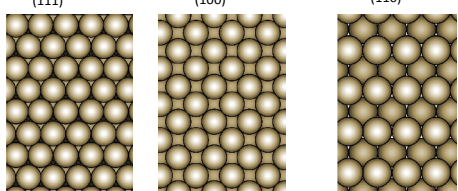
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### (111), (100), (110) FCC kristala



(111) (100) (110)

Idealne površine

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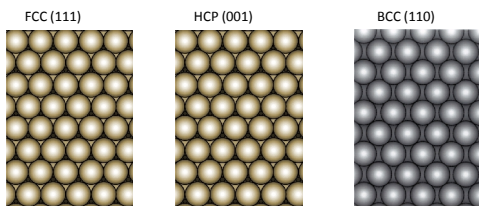
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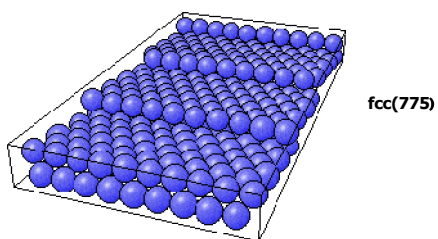
Gusto pakovne površine FCC, BCC, HCP kristala imajo približno heksagonalni raspored atoma



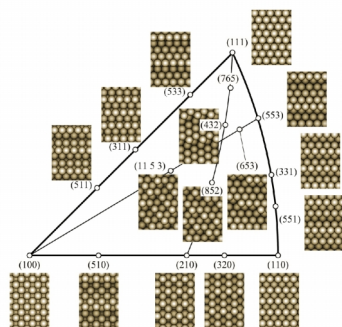
67

**Površine visokih Milerovih indeksa:**

**Terasa + stepenik**

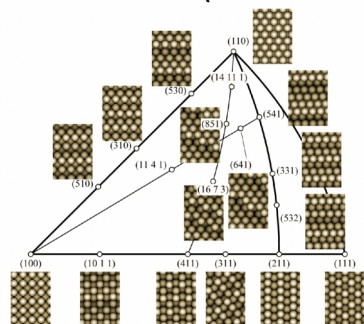


## Opšta slika FCC



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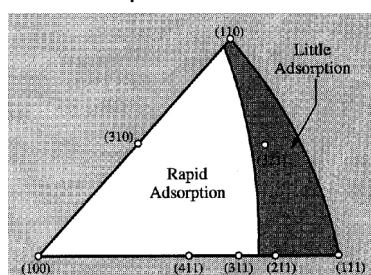
## Opšta slika BCC (slično kao FCC)



BCC (LMN) = FCC (L, M+N, M-N)

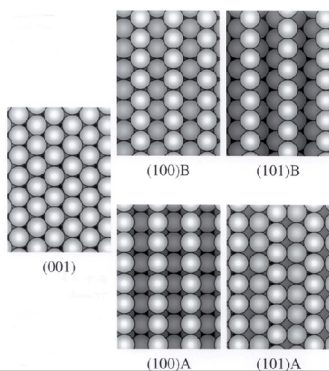
70

## Reaktivnost zavisi od orijentacije površine



The rate of adsorption of nitrogen on tungsten as a function of the position of the plane within the stereographic triangle. (Data of Ehrlich and Hudda [1963], Delchar and Ehrlich [1965], and Adams and Germer [1971].)

## HCP je malo drugačija



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## Rekonstrukcija i relaksacija površine

Idealna površina je samo aproksimacija

Dva tipa strukturnih promena: relaksacija i rekonstrukcija

Kod relaksacije promene su male, periodika ćelije nije promenjena

Kod rekonstrukcije velike strukturne promene, promena periodike jedinične ćelije površine u odnosu na dubinu materijala, izraženije kod kovalentnih kristala

Može biti indukovana adsorbatom

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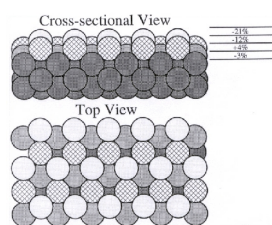
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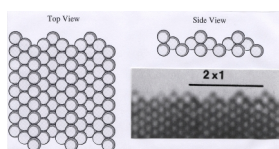
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## Relaksacija: Obično opada rastojanje između površinskih slojeva



Rekonstrukcija: preraspodela atoma da se površina oslobodi nezasićenih površinskih veza




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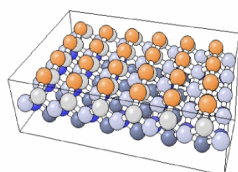
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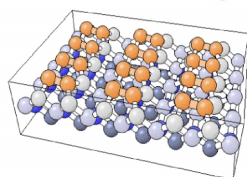
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## Si(100)-(2x1)



A. Unreconstructed Si(100)-(1x1) surface.

The Si atoms of the topmost layer are highlighted in orange; these atoms are bonded to only two other Si atoms, both of which are in the second layer (shaded grey).



B. Reconstructed Si(100)-(2x1) surface.

The Si atoms of the topmost layer form a covalent bond with an adjacent surface atom; are thus drawn together as pairs; they are said to form "dimers".

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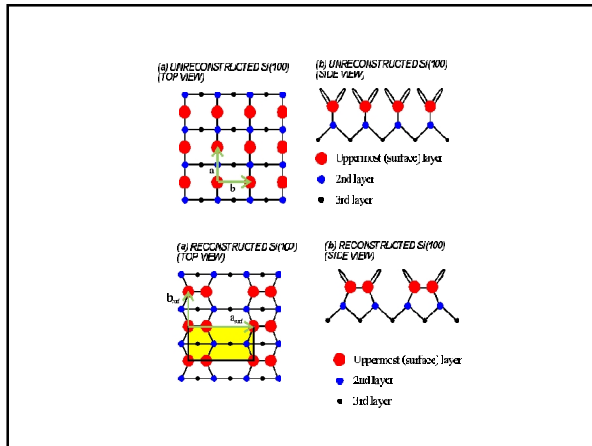
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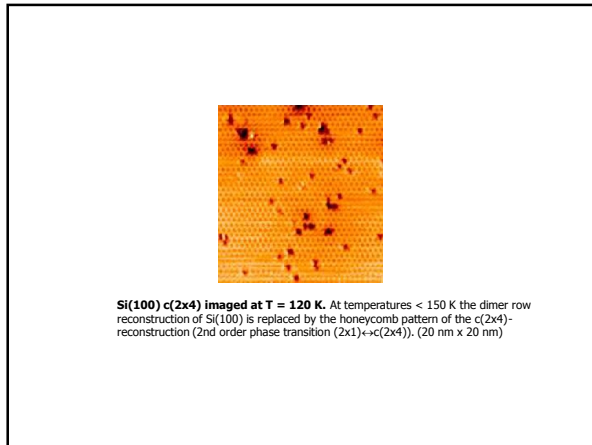
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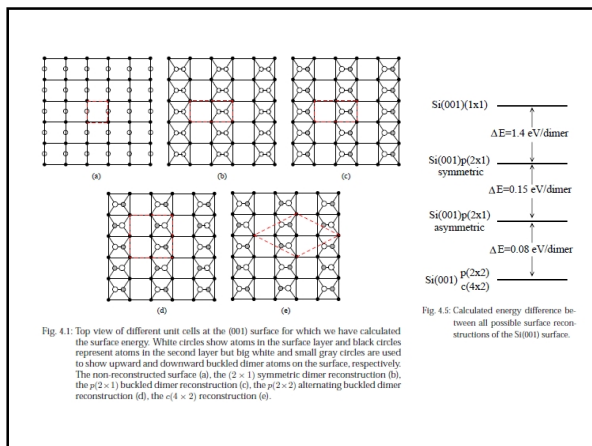
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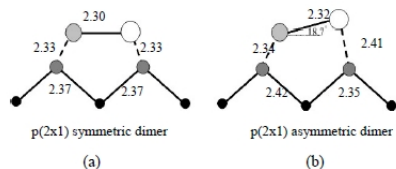
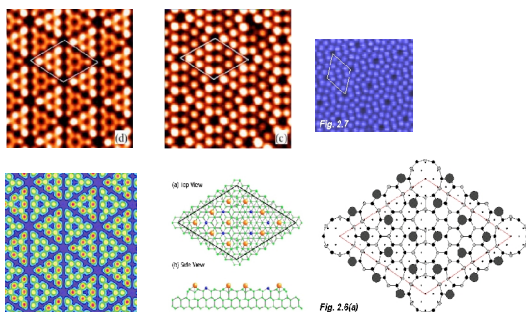
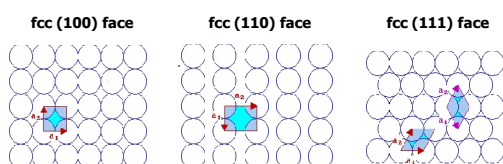


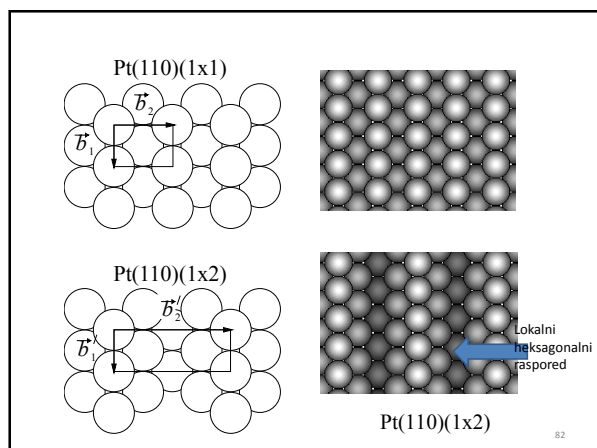
Fig. 4.2: Bond length of symmetric dimer structure (a), the bond length and the angle of the buckled dimer structure (b).

### Si(111)-(7x7)



### Wood-ova notacija: površinske strukture






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## Adsorpcija

- Šta je pokreće
- Kako izgledaju adsorbovani slojevi
- Adsorpcioni trendovi

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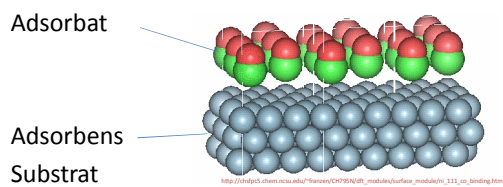
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## Key Terms




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## Overview

Fizičke sile - fizisorpcija

Dipol-dipol

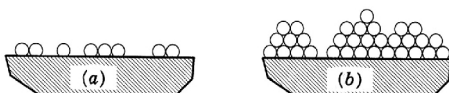
korelacija

Hemijske sile – hemisorpcija

preraspodela naelektrisanja

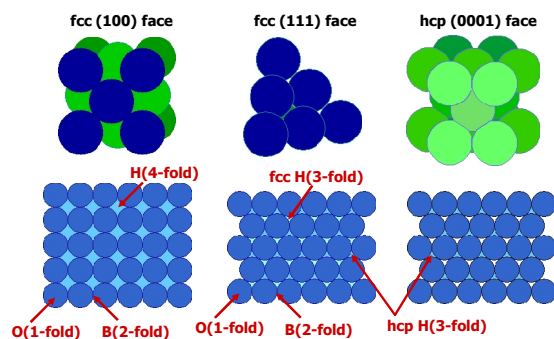
Gustine slične tečnostima

$(1 \text{ gm/cm}^3) = 10^{15} \text{ molekula/cm}^2$



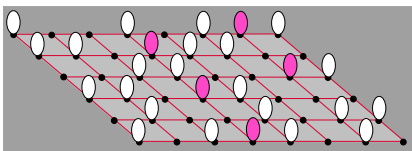
85

## Adsorpciona mesta



## Geometrija adsorbovanih slojeva

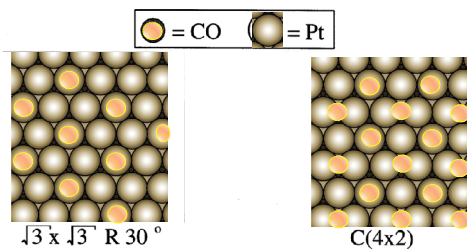
Struktura adsorbovanih slojeva je uslovljena strukturom substrata



Langmirovov tip adsorpcije na čvrstoj površini

87

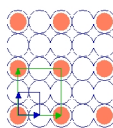
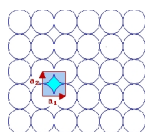
## CO na Pt(111)



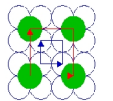
Crossley &amp; King [1980]

88

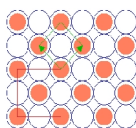
## fcc (100) face



Substrate : fcc(100)  
Substrate unit cell  
Adsorbate unit cell

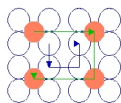
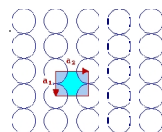


Substrate : fcc(100)  
Substrate unit cell  
Adsorbate unit cell

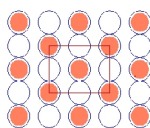


Substrate : fcc(100)  
 $\sqrt{2} \times \sqrt{2}$   
 $(\sqrt{2} \times \sqrt{2})R45$

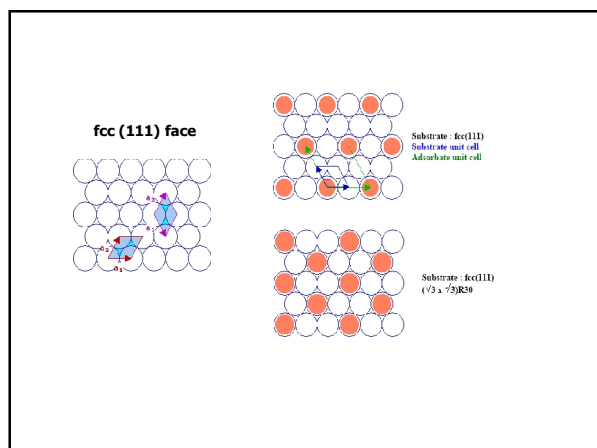
## fcc (110) face



Substrate : fcc(110)  
Substrate unit cell  
Adsorbate unit cell



Substrate : fcc(110)  
 $\sqrt{2} \times \sqrt{2}$




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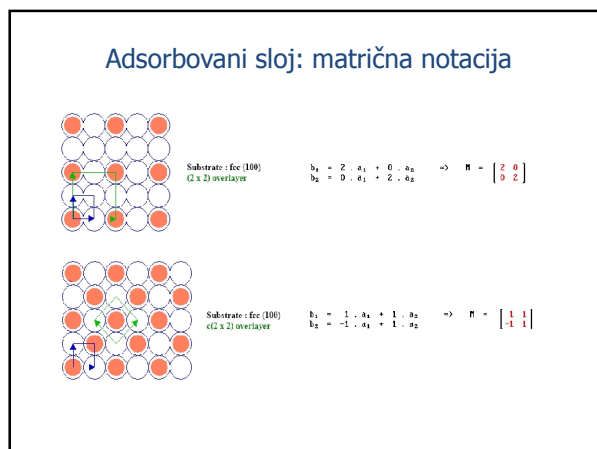
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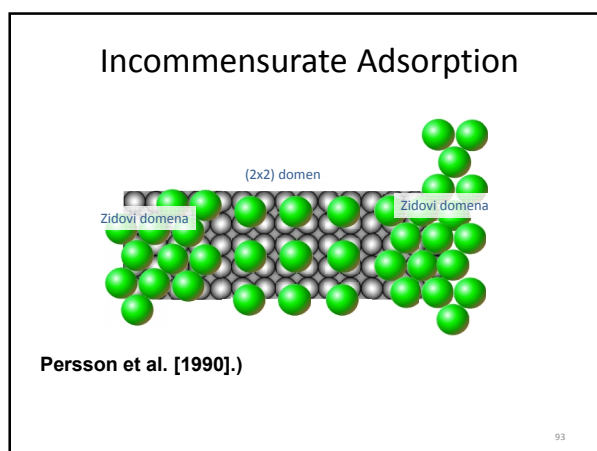
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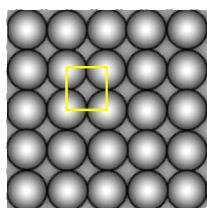
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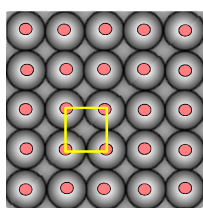
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## Kvadratna rešetka



primitive unit cell



p(1x1)

94

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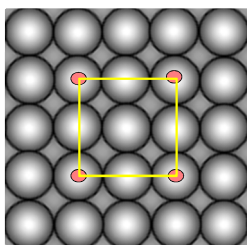
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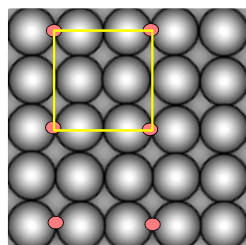
## Kvadratna rešetka

c



p(2x2)

d



p(2x2)

95

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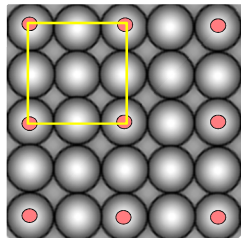
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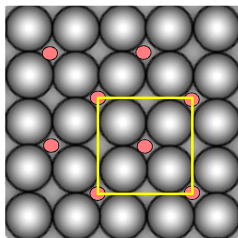
## Primitivna i centrirana rešetka

c



p(2x2)

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c(2x2)

96

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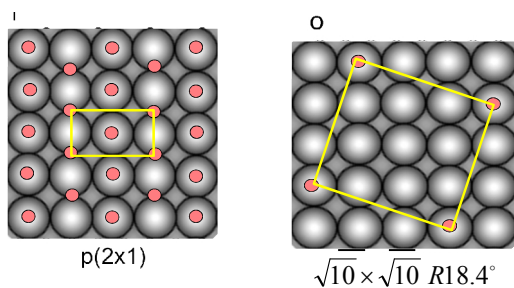
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## Kvadratna rešetka



97

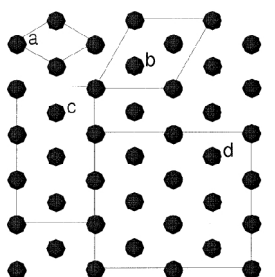
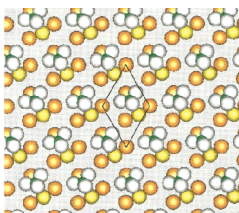
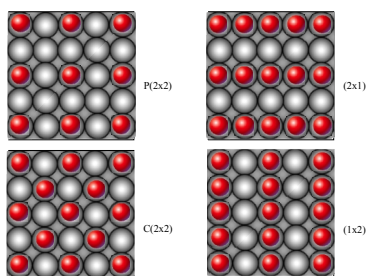
CH<sub>3</sub>S/Au(111)

Figure 1. Surface cells used in the calculations. (a)  $1 \times 1$ ; (b)  $(\sqrt{3} \times \sqrt{3})R30$ ; (c)  $3 \times 3$ ; (d)  $1/3 (3 \times 3)$ . These cells contain 1, 3, 6 and 17 Au atoms per layer, respectively. Cell (d) corresponds to the  $c(4 \times 2)$  superlattice of the  $(\sqrt{3} \times \sqrt{3})R30$  lattice.

| $\Theta$ | site       | $\Delta E$ | S-M  | $E_{\text{ads}}$ | cell |
|----------|------------|------------|------|------------------|------|
| 1        | ~on-top    | 2.84       | 3.00 | 4.4              | c    |
| 1        | ~on-top    | 2.86       | 3.00 | 5.3              | d    |
| 0.5      | ~on-top    | 2.84       | 2.98 | 5.9              | d    |
| 1        | fcc hollow | 1.81       | 2.59 | 2.9              | b    |
| 0.5      | fcc hollow | 1.60       | 2.51 | 11.5             | c    |
| 0.25     | fcc hollow | 1.59       | 2.51 | 18.3             | d    |
| 1        | hcp hollow | 1.90       | 2.60 | -1.1             | b    |
| 0.5      | hcp hollow | 1.70       | 2.53 | 4.7              | c    |
| 1        | bridge     | 2.06       | 2.57 | 18.6             | b    |
| 0.5      | bridge     | 2.07       | 2.50 | 19.6             | c    |
| 0.25     | bridge     | 2.05       | 2.49 | 21.0             | d    |



## Adsorpcija CO na kvadratnoj rešetki – adsorbovane faze



The absorption of molecules in a p(2x2), c(2x2), (2x1) overlayer. The dark circles represent sites, the red circles represent adsorption on the sites.

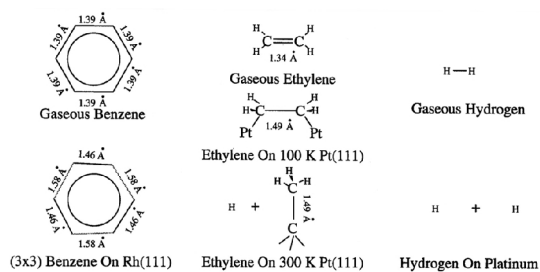
## Hemisorpcija na metalima

- Metali imaju mnogo slobodnih elektrona koji učestvuju u vezivanju
- Veza je delokalizovana
- Elektroni su pokretni

100

Adsorpcija je kompromis – da bude dobro i adsorbatu i substratu

Mehanizam aktivacije hemijske veze u katalizi



101

## Trendovi u periodnom sistemu

# Periodic Table of the Elements

hydrogen

alkali metals

alkali earth metals

transition metals

poor metals

nonmetals

noble gases

rare earth metals

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |    |    |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|----|----|
| H  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    | He |    |    |   |   |    |    |
| Li | Be |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    | Na |    |   |   |    |    |
| Na | Mg |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    | Al | Si | P | S | Cl | Ar |
| K  | Ca | Sc | Ti | V  | Cr | Mn | Fe | Co | Ni | Cu | Zn | Ga | Ge | As | Se | Br | Kr |    |    |   |   |    |    |
| Rb | Sr | Y  | Zr | Nb | Mo | Tc | Ru | Rh | Pd | Ag | Cd | In | Sn | Sb | Te | I  | Xe |    |    |   |   |    |    |
| Cs | Ba | La | Hf | Ta | W  | Re | Os | Ir | Pt | Au | Hg | Tl | Pb | Bi | Po | At | Rn |    |    |   |   |    |    |
| Fr | Ra | Ac | Th | Pa | U  | Np | Pu | Am | Cm | Bk | Cf | Es | Fm | Md | No | Lr |    |    |    |   |   |    |    |

58

59

60

61

62

63

64

65

66

67

68

69

70

71

Ce

Pr

Nd

Pm

Sm

Eu

Gd

Tb

Dy

Ho

Er

Tm

Yb

Lu

90

91

92

93

94

95

96

97

98

99

100

101

102

103

Th

Pa

U

Np

Pu

Am

Cm

Bk

Cf

Es

Fm

Md

No

Lr

102



## Kvalitativni aspekti

|                                | Adsorbing Gas  |                |                |        |
|--------------------------------|----------------|----------------|----------------|--------|
| Metal                          | H <sub>2</sub> | O <sub>2</sub> | N <sub>2</sub> | CO     |
| Si, Ge                         | 0 or 2         | 3              | 0              | 0      |
| InP                            | 0              | 3              | 0              | 0      |
| NiO                            | 0              | 1              | ?              | 1      |
| ZnO                            | def-3          | def-3          | ?              | 1      |
| MgO                            | 0              | 1              |                |        |
| Al <sub>2</sub> O <sub>3</sub> | 0              | 1              |                |        |
| SiO <sub>2</sub>               | def-2          | def-3          |                |        |
| NaCl                           | 0              | ?              | 1              | 0-100K |
| LiF                            |                |                |                | 1-40 K |

- 0 – nema adsorpcije  
 1 – ima na 100 K ali nema na 300 K  
 2 – aktivirani proces  
 3 – brza adsorpcija na sobnoj temperaturi

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## Kvalitativni aspekti

| Metal     | C <sub>2</sub> H <sub>2</sub><br>C <sub>2</sub> H <sub>4</sub>     | CH <sub>4</sub><br>C <sub>2</sub> H <sub>6</sub> | CH <sub>3</sub> OH | H <sub>2</sub> O |
|-----------|--------------------------------------------------------------------|--------------------------------------------------|--------------------|------------------|
| Group a   | 3                                                                  | ?                                                | ?                  | 3                |
| Group b   | 3                                                                  | 2                                                | 3                  | ?                |
| Group c   | 3                                                                  | ?                                                | 3                  | 1                |
| Group d   | 3                                                                  | 2                                                | 3                  | 1                |
| Group e   | 3                                                                  | 2                                                | 3                  | 1                |
| Cu        | 1 or 3                                                             | 0                                                | 1                  | 1                |
| Ag        | 1                                                                  | 0                                                | 1                  | 1                |
| Au        | 3                                                                  | 0                                                | 1                  | 1                |
| Al        | 2                                                                  | ?                                                | 3                  | 3                |
| K, Na, Li | 3 C <sub>2</sub> H <sub>2</sub><br>0 C <sub>2</sub> H <sub>4</sub> | ?                                                | ?                  | 3                |

- 0 – nema adsorpcije  
 1 – ima na 100 K ali nema na 300 K  
 2 – aktivirani proces  
 3 – brza adsorpcija na sobnoj temperaturi

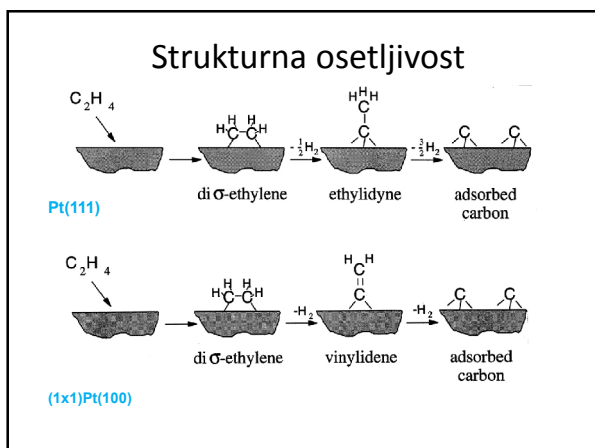
107

## Molekulska i disocijativna adsorpcija Brodén et al. [1976]

10<sup>-6</sup> torr

| Gas            | 300 K                     |                           | 300 K                     |                           | 100 K                     |                           | 100 K                     |                           |
|----------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|
|                | Disociated                | Molecular                 | Disociated                | Activated                 | Disociated                | Molecular                 | Disociated                | Molecular                 |
| CO             | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu |
| N <sub>2</sub> | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu |
| O <sub>2</sub> | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu |
| NO             | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu | Sc Ti V Cr Mn Fe Co Ni Cu |

| Key                    |  | Molecular And Dissociative Adsorption |  | Activated Dissociative Adsorption |  | No Adsorption |  | Limited Data |  |
|------------------------|--|---------------------------------------|--|-----------------------------------|--|---------------|--|--------------|--|
| Disociative Adsorption |  | Molecular Adsorption                  |  | Activated Dissociative Adsorption |  | No Adsorption |  | Limited Data |  |




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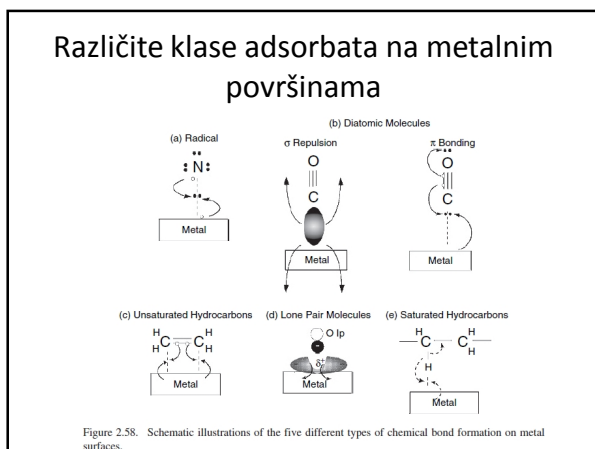
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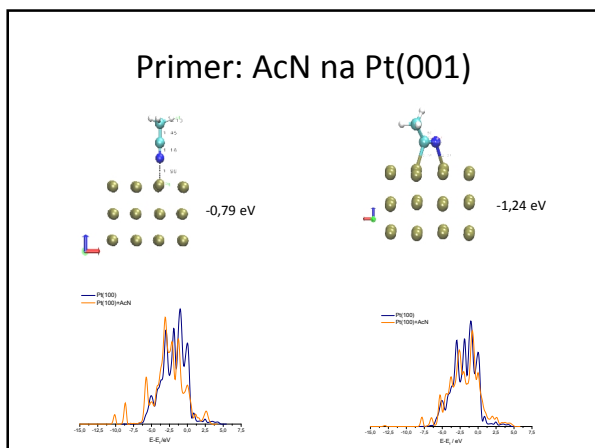
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## Korelacija sa elektronskom strukturom

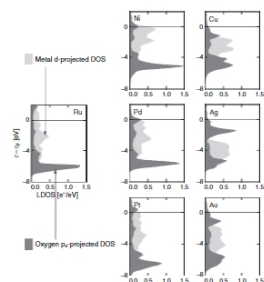


Figure 4.2. The density of states projected onto the d states of the surface atoms for the surfaces considered in Figure 4.1 (grey). Also shown (black) is the oxygen 2p<sub>z</sub> projected density of states for O adsorbed on the same surface. The formation of bonding and anti-bonding states below and above the metal d states is clearly seen. Adapted from Ref. [4].

## Korelacija sa elektronskom strukturom

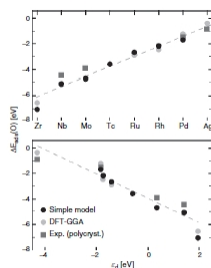
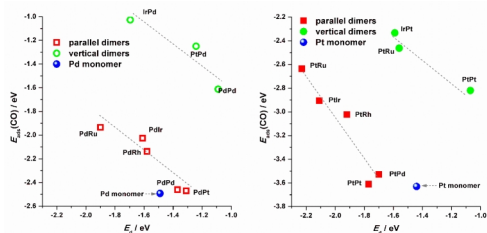
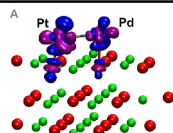


Figure 4.6. Variations in the O adsorption energy along the 4d transition metal series. The results of full DFT calculations are compared to those from the simple d band model and to experiments. Below the same data are plotted as a function of the d band center. Adapted from Ref. [4].

Energije adsorpcije mnogih jednostavnih adsorbata se korelišu sa centrom d-trake metalnog substrata

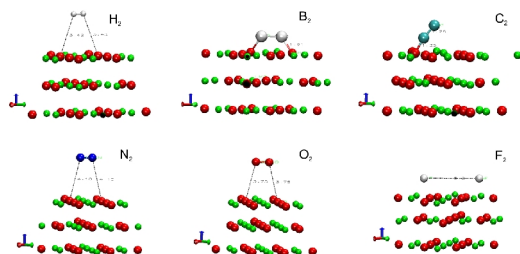
Adsorpcija na nisko-koordinisanim metalnim atomima (defekti, kinkovi, stepenice, adsorbovani klasteri – katalizatori!)

Nema jedinstvene teorije



Adsorpcija na oksidima – nema jedinstvene teorije  
Primer:  $X_2@MgO(001)$

Svojstva jonskih kristala!!!




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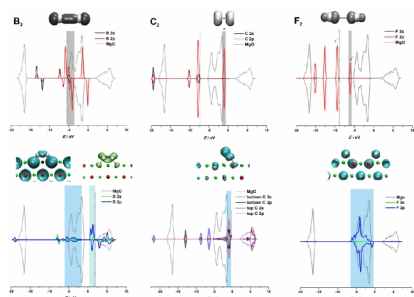
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Adsorpcija na oksidima – nema jedinstvene teorije  
Primer:  $C_2@MgO(001)$




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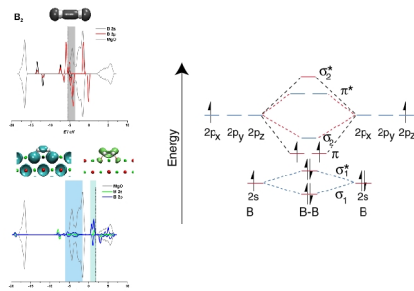
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Adsorpcija na oksidima – nema jedinstvene teorije  
Primer:  $B_2@MgO(001)$




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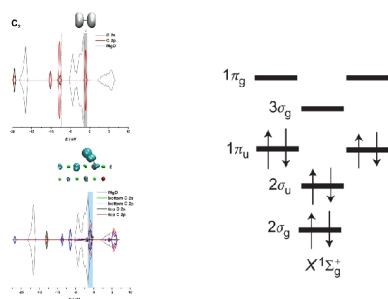
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Adsorpcija na oksidima – nema jedinstvene teorije  
Primer:  $C_2@MgO(001)$




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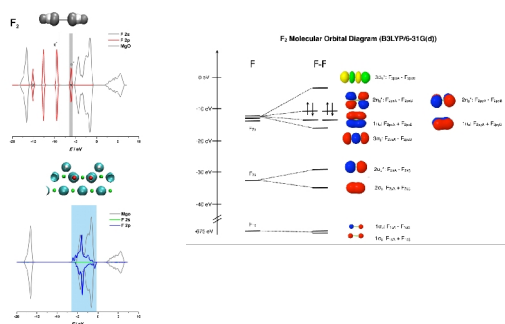
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Adsorpcija na oksidima – nema jedinstvene teorije  
Primer:  $F_2@MgO(001)$




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