## Matlab Basics for Math 283

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Matlab has tutorials available online at:
http://www.mathworks.com/academia/student_center/tutorials/launchpad.html

## Starting up matlab:

Go to finder -> applications -> matlab701 -> matlab7.01 [Pick the current version] From a terminal command prompt:
matlab (display matlab desktop, access editor, helpdesk)
matlab -nojvm (no java virtual machine, no desktop -- faster)
matlab -nodisplay (no desktop, no plot windows -- faster)
matlab -help (to see all options)

NOTE: ">>" is the matlab prompt.

## Operators, Punctuation

Operators
Arithmetic operators in matlab:

$$
\begin{array}{|l|l|l|l|l}
\hline * & I & + & - & \wedge
\end{array}
$$

follow the convention in linear algebra. Matrices must have correct dimensions for any operation. Follows order of operations. Use parentheses to change precedence >> 1*2/3+4^5-4^5
ans $=$
0.6667

Element-by-element operators operate on arrays or matrices by element (essentially operator preceded by a period):


```
>> [llll}10\mp@code{2 3.*[llll
ans =
```

| Matrix Operations |  | Array Operations |  |
| :---: | :---: | :---: | :---: |
| x | $\begin{aligned} & 1 \\ & 2 \\ & 3 \end{aligned}$ | y | $\begin{aligned} & 4 \\ & 5 \\ & 6 \end{aligned}$ |
| $\mathrm{x}^{\prime}$ | 123 | $y^{\prime}$ | 456 |
| $x+y$ | $\begin{aligned} & 5 \\ & 7 \\ & 9 \end{aligned}$ | $x-y$ | $\begin{aligned} & -3 \\ & -3 \\ & -3 \end{aligned}$ |
| $x+2$ | $\begin{aligned} & 3 \\ & 4 \\ & 5 \end{aligned}$ | x-2 | $\begin{gathered} -1 \\ 0 \\ 1 \end{gathered}$ |
| $x^{*} y$ | Error | x.*y | $\begin{aligned} & 4 \\ & 10 \\ & 18 \end{aligned}$ |
| $x^{\prime *} y$ | 32 | $x^{\prime} .{ }^{*} \mathrm{y}$ | Error |
| $x^{*} y^{\prime}$ | $\begin{aligned} & 456 \\ & 81012 \\ & 121518 \end{aligned}$ | x. ${ }^{*} y^{\prime}$ | Error |
| $\mathrm{x}^{*} 2$ | $\begin{aligned} & 2 \\ & 4 \\ & 6 \end{aligned}$ | x.*2 | $\begin{aligned} & 2 \\ & 4 \\ & 6 \end{aligned}$ |
| xly | 16/7 | x.ly | $\begin{aligned} & 4 \\ & 5 / 2 \\ & 2 \end{aligned}$ |
| 21x | $\begin{aligned} & 1 / 2 \\ & 1 \\ & 3 / 2 \end{aligned}$ | 2./x | $\begin{aligned} & 2 \\ & 1 \\ & 2 / 3 \end{aligned}$ |
| x/y | $\begin{array}{lll} 0 & 0 & 1 / 6 \\ 0 & 0 & 1 / 3 \\ 0 & 0 & 1 / 2 \end{array}$ | x./y | $\begin{aligned} & 1 / 4 \\ & 2 / 5 \\ & 1 / 2 \end{aligned}$ |
| x/2 | $\begin{aligned} & 1 / 2 \\ & 1 \\ & 3 / 2 \end{aligned}$ | x./2 | $\begin{aligned} & 1 / 2 \\ & 1 \\ & 3 / 2 \end{aligned}$ |
| $x^{\wedge} y$ | Error | $x . \wedge y$ | $\begin{aligned} & 1 \\ & 32 \\ & 729 \end{aligned}$ |
| $x^{\wedge} 2$ | Error | x.^2 | $\begin{aligned} & 1 \\ & 4 \\ & 9 \end{aligned}$ |
| $2^{\wedge} x$ | Error | 2.^x | $\begin{aligned} & 2 \\ & 4 \\ & 8 \end{aligned}$ |

## Matlab Punctuation

| \% | Denotes comment line. Information after \% is ignored by matlab. <br> >> \%nothing happens <br> >> |
| :---: | :---: |
| , | Comma works like blank space. Concatenates array elems along row. Shows results. $\begin{aligned} & \gg x=[1,2,3], \\ & x=1 \end{aligned}$ |
| ; | Concatenates array elements along column. Suppresses printing contents of variable to screen. $\begin{aligned} & \text { >> x=[1;2;3] } \\ & x= \\ & \\ & \quad 1 \\ & 2 \\ & 3 \\ & \gg x=[1 ; 2 ; 3] ; \\ & \text { >> } \end{aligned}$ |
| : | Specifies a range of numbers. A colon in an array dimension accesses all elements in that dimension. ```>> z=[1:0.25:2; 3:0.25:4] % row 1: 1 to 2, row 2: 3 to 4, step size/increment by 0.25 z = lllll >> z(:,2) %all rows, column 2 ans = 1.2500 3.2500 >> z(1,:) %all columns, row 1 ans = 1.0000 1.2500 1.5000 1.7500 2.0000``` |
| ' | Apostrophe at the end of a vector or matrix gives its transpose. ```>> z(:,2)' ans = 1.2500 3.2500``` |

More basic operators/functions

| exp | log | log10 | log2 | sqrt |
| :--- | :--- | :--- | :--- | :--- |

## Basic Data Structures

Basic data constructs are arrays and matrices.
Arrays can be row vectors ( 1 by $n$ array) or column vectors ( $n$ by 1 array).
A matrix can have two dimensions (example: $m$ rows and $n$ columns). Multi-dimensional arrays can also be specified.

```
>> row vect = [1 4 5}
>> column_vect = [1;4;5];
```

Concatenate column vectors along same row:

```
>> two_column_vect = [column_vect column_vect]
two_column_vect =
    1 - 
    4
```

Concatenate row vectors along same column:

```
>> two_row_vect = [row_vect; row_vect]
two_row_vect =
    1 4 5
    1 4 5
```


## Accessing array elements

| $\mathbf{a}(\mathrm{i})$ | i-th element of array a. |
| :--- | :--- |
| $\mathbf{A}(\mathrm{i},: \mathbf{)}$ | $\left.\begin{array}{l}\text { i-th row of a matrix } \mathbf{A}, \text { all columns (Can select certain columns by } \\ \text { putting an array of indices instead of ' }: '\end{array}\right)$. |

Array building

| zeros, ones | Builds arrays with all 0's or all 1's respectively. <br> $\gg x=\operatorname{zeros}(1,3)$ <br> $x=$ |
| :--- | :--- |
| eye | Creates an identity matrix. <br> $\gg x=$ <br> $x=$ <br> $x$ |
|  | 1 <br> 0 |
|  | 0 |

Some basic functions on arrays and matrices
Type 'help function_name' for details on usage.

| size | max | min | mean | std | var | sort | sum | prod | diff | dot |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| cross |  |  |  |  |  |  |  |  |  |  |
| Not covered: cell arrays. |  |  |  |  |  |  |  |  |  |  |

## File and Workspace Management, File I/O

| File and workspace management |  |
| :--- | :--- |
| dir, Is | Show files in active directory |
| delete filename | Remove file filename in active directory. |
| cd, pwd | Show present directory |
| cd dir | Changes the directory to dir |
| clear | Remove all variables from workplace |
| clear $\mathbf{x}$ | Remove variable x from the workplace. |
| who | List all variables in the workspace |


| le I/ |  |
| :---: | :---: |
| load | Syntax: load filename <br> Load from file. Check out variations of use. File should have correct format (Same number of columns for each row, rows for each column) and no nonnumeric characters. For instance if you have a file called test.dat in current dir: ```>> load test.dat >> test test = 1 2 3``` |
| save | Syntax: save filename variable -ascii Saves 'variable' in ASCII format in'filename' >> save test copy.dat test -ascii |

## Control Flow

## Conditional Control - if, else, elseif, and switch/case

if, else, and elseif
if evaluates a logical expression and executes a group of statements based on the value of the expression. In its simplest form, its syntax is

```
if logical_expression
    statements
end
```

The else and elseif statements further conditionalize the if statement:

The else statement has no logical condition. The statements associated with it execute if the preceding if (and possibly elseif condition) evaluates to logical 0 (false).

The elseif statement has a logical condition that it evaluates if the preceding if (and possibly elseif condition) is false. The statements associated with it execute if its logical condition evaluates to logical 1 (true). You can have multiple elseif statements within an if block.

For some value of n :

```
if n < 0 % If n negative, display message.
    disp('Input negative');
elseif n == 0 % If n equals zero
    disp('Input zero');
else %n greater than zero is remaining case
    disp('Input positive');
end
```

switch, case, and otherwise
switch executes certain statements based on the value of a variable or expression. Its basic form is

```
switch expression (scalar or string)
    case valuel
        statements % Executes if expression is valuel
    case value2
        statements % Executes if expression is value2
    .
    otherwise
        statements % Executes if expression does not
        % match any case
end
```

* More about the difference between switch and if/elseif: http://goo.gl/dpulZ


## Loop control - for, while, break

## for

The for loop executes a statement or group of statements a predetermined number of times. Its syntax is

```
for index = start:increment:end
    statements
end
```

The default increment is 1 . You can specify any increment, including a negative one. For positive indices, execution terminates when the value of the index exceeds the end value; for negative increments, it terminates when the index is less than the end value.

For example, this loop executes five times.

```
x=[1:10];
for n = 2:6
    x(n) = 2 * x(n);
```

end
while

The while loop executes a statement or group of statements repeatedly as long as the controlling expression is true (1). Its syntax is:
while expression
statements
end

If the expression evaluates to a matrix, all its elements must be 1 for execution to continue. To reduce a matrix to a scalar value, use the all and any functions.

Increments n from 0 to 10:

```
n = 0;
while n < 10
    n = n + 1
```

end

Exit a while loop at any time using the break statement. Useless example that breaks at $n==5$ :
$\mathrm{n}=0$;
while n < 10
$\mathrm{n}=\mathrm{n}+1$;
if $\mathrm{n}==5$, break, end
end

## Simple Plots

## Basic commands

| plot | Draws plot of two equal-sized vectors x,y. Style is specified by character <br> string s where s could be for example 'b*' for blue asterisk or 'bd' for <br> blue diamonds representing points. Default is blue line with points <br> connected. Usage: plot $(x, y)$ or plot (x,y, s) |
| :--- | :--- |
| hist | Draws histogram of input array. Default number of bins is 10. Usage: <br> hist (array) or hist (array, num_bins) |
| xlabel | Label for x-axis. Usage: xlabel ('x axis variable') |
| ylabel | Label for y-axis. Usage: xlabel ('y axis variable') |
| axis | Set specified x- and y-axis limits. Usage: axis ([xmin xmax ymin <br> ymax]) |
| xlim | Set x-axis limits only. Usage: xlim ([xmin xmax]) |
| ylim | Set y-axis limits only. Usage: ylim ([ymin ymax]) |
| title | Title over plot. Usage: title ('plot title') |
| hold on, <br> off | 'hold on' causes subsequent plots to be superimposed on current one, <br> whereas 'hold off' specifies each new plot start afresh. Default is off. |
| figure | Creates a new figure window. Usage: figure; |

## Saving plots

Save plots in desired format using the figure window (File -> Save as). To save the plot on the current figure window as a png file using the command line,type:
>>print(gcf, '-dpng', '-r0', 'plot_filename');

## More plotting function examples

Type 'help function_name' for details on usage.

| loglog semilogx | semilogy | plotyy | bar | scatter | pie |
| :--- | :---: | :---: | :---: | :---: | :---: |

## Scripts and Functions

An M-file is a text file that contains MATLAB commands and has a .m filename extension. Use Matlab Editor/Debugger or any text editor (emacs, vi) to create function.m or script.m file. To start in MATLAB, go to File->New-> M-file
Note that the name of the function or script filename is identical to the command invoked at MATLAB prompt (without the .m extension).
Script M-files No input or output arguments and operate on variables in the workspace. Just a series of commands. Example: script.m


```
>> x = [-3:.1:3]
>> y = x .^ 2;
plot(x,y);
>> xlabel('x');
>> ylabel('y');
>> title('parabola y = x^2');
>> print(gcf,'-dpng','-r0','parabola.png');
>> print(gcf,'-depsc','parabola.eps');
```

```
% script.m
% series of matlab commands in a file.
x = [1:10]
mean(x)
```

Function M-files Contain a function definition line and can accept input arguments and return output arguments, and their internal variables are local to the function (unless declared global). Syntax requires the first line to be of form:

```
function [out1, ..., outN] = func_name(in1, ..., inN)
```

Example: stats_wrapper.m

```
function [mean_x, var_x] = stats_wrapper(x)
\%stats_wrapper.m
\%computes the mean and variance of array \(x\)
mean \(x=\operatorname{mean}(x)\)
\(\operatorname{var} \overline{\mathrm{x}}=\operatorname{var}(\mathrm{x})\);
Example usage:
>> \([m, v]=\) stats_wrapper \(([1,2,3,4,5])\)
\(\mathrm{m}=\)
    3
\(\mathrm{V}=\)
    2.5000
```


## Statistics in Matlab

List of functions by category:
http://www.mathworks.com/access/helpdesk/help/toolbox/stats/

## Examples:

## Some CDF, PDF, Inverse functions, Random number generators

| $\underline{\text { normcdf }}$ | Normal (Gaussian) cdf given value and parameters |
| :--- | :--- |
| $\underline{\text { poisscdf }}$ | Poisson cdf given value and parameters |
| $\underline{\text { binopdf }}$ | Binomial pdf given value and parameters |
| $\underline{\text { geopdf }}$ | Geometric pdf given value and parameters |
| $\underline{\text { norminv }}$ | Normal (Gaussian) critical values given p and parameters |
| $\underline{\text { poissinv }}$ | Poisson critical values given p and parameters. |
| $\underline{\text { normrnd }}$ | Normal (Gaussian) random numbers given parameters |
| $\underline{\text { poissrnd }}$ |  |

## Some Hypothesis Tests

| $\frac{\text { ranksum }}{\text { signrank }}$ | Wilcoxon rank sum test |
| :--- | :--- |
| $\frac{\text { signtest }}{\text { ttest }}$ | Wilcoxon signed rank test |
| $\frac{\text { ttest2 }}{\text { ztest }}$ | Sign test for paired samples |
| $\underline{y}$ | One sample t-test |
|  | Two sample t-test |
|  | Z-test |

## help function name

Best way to know how to correctly use built-in function and understand what it is doing.

## Sources:

1. Highham, D.J., and Higham, N.J. Matlab Guide. SIAM, Philadelphia, 2000.
2. Martinez, W.L., and Martinez, A.R. Appendix A, Computational Statistics Handbook With Matlab. Chapman\&Hall/CRC, New York, 2002.
3. http://www.mathworks.com/access/helpdesk/help/techdoc/matlab.html
4. 

http://www.mathworks.com/access/helpdesk/help/toolbox/stats/stats product page.html

## Exercises:

## Generate values from a binomial distribution

\% Generate 10,000 random values from a binomial distribution and store in row vector
\% empirical_bino. Use help to figure out input values for binornd.
>>empirical_bino = binornd(100,1/2,1,10000);
\%Check that the mean and variance are close to that of the distribution from which it was $\%$ generated.
>> mean(empirical_bino)
>> var(empirical_bino)
\% Since binomial with $p=1 / 2$ is symmetric, check that median is also near true mean.
>> median(empirical_bino)
\% Check out the distribution of the values in empirical_bino by plotting the histogram. \% Default number of bins is 10.
>>hist(empirical_bino)
\% Use hold on to draw/trace plot of the distribution over the histogram.
>>[frequency, bins] = hist(empirical_bino);
>>hold on;
>>plot(bins, frequency, 'b*'); \%use blue asterisk
>>xlabel('bins');
>>ylabel('counts');
>>title('Simulated distribution');
>>binsize=bins(2)-bins (1) ;
>>plot(0:100, 10000*binsize*binopdf(0:100, 100, 1/2),'r');

## What does it look like?

\% Working with the cdf
\% Get the probability that values from $B(0,1)$ are less than or equal to the mean \% of the values in empirical_bino. Do the same for the median.

## \% First, check what we know

>> binocdf (50,100,1/2)
>> pmean $=$ binocdf(mean(empirical_bino), 100,1/2)
>> pmedian $=$ binocdf(median(empirical_bino), 100,1/2)
\% Use the cdf to get back the critical values
\% corresponding to those probability cutoffs.
\% First, check what we know
>> binoinv (0.5, 100,1/2)
>> binoinv(pmean, 100,1/2)
>> binoinv(pmedian, 100,1/2)
\% Plot the cdf of empirical_bino
\% Need to sort the values in empirical_bino from low to high and
\% get the corresponding probability $P x=P(X<=x)$ for each value in the
$\%$ array according to the theoretical distribution.
>> Px = binocdf(sort(empirical_bino), 100,1/2);
\% Use Figure to create a new window
>>figure;
\% Plot the sorted values of empirical_bino on x-axis and \% corresponding theoretical probabilities on $y$-axis.

```
>>plot(sort(empirical_bino), Px)
```

>>xlabel('x')
>>ylabel('P_x');
>>title('cdf of empirical bino');

## Odds and Ends

\%because we can let us practice file i/o with pmean
>> save pmean_file pmean -ascii
>> load pmean_file
>> pmean_file
>> delete pmean_file

## Function example

Create simple function called sim_bino.m that plots the distribution of $m$ values generated from a binomial distribution with parameters $n$ and $p$ and returns the mean and variance of the observed distribution.
\% Calls sim_bino with parameters $n=100, p=1, m=100000$ and saves plot as test.png \% Note that the character string 'test' is in single quotes.
>>[obs_mean, obs_var] = sim_bino(100,1/2,10000, 'test')
File: sim_bino.m
function [obs_mean, obs_var] = sim_bino(n, p, m, plotname) \%sim_bino.m
\%--
\% Simple function that plots distribution of $m$ values from a binomial distribution with
\% parameters n and p and saves this plot in PNG as 'plotname' in the current directory.

```
empirical_bino = binornd(n, p, 1, m);
figure;
hist(empirical_bino);
[frequency, bins] = hist(empirical_bino);
hold on;
plot(bins, frequency, 'b-*'); %use blue line and asterisk
xlabel('bins');
ylabel('counts');
title('Simulated distribution');
%save plot as plotname.png
print(gcf, '-dpng', '-r0',plotname);
obs_mean = mean(empirical_bino);
obs_var = var(empirical_bino);
```

