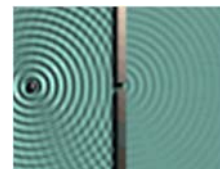
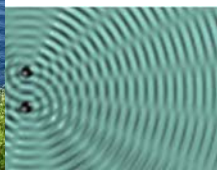


# Nove fizickohemijske metode

Ivana Radosavljevic Evans  
Durham University, UK



# Nove fizickohemijske metode:

## Metode zasnovane na sinhrotronskom zracenju

### ➤ Plan predavanja:

- Difrakcione metode strukturne karakterizacije materijala
- Oblasti primene difrakcije sinhrotronskog X-zracenja
- Eksperimentalni aspekti difrakcije sinhrotronskog X-zracenja
- Prednosti (i mane) u odnosu na laboratorijski XRD
- Primeri studija neorganskih funkcionalnih materijala

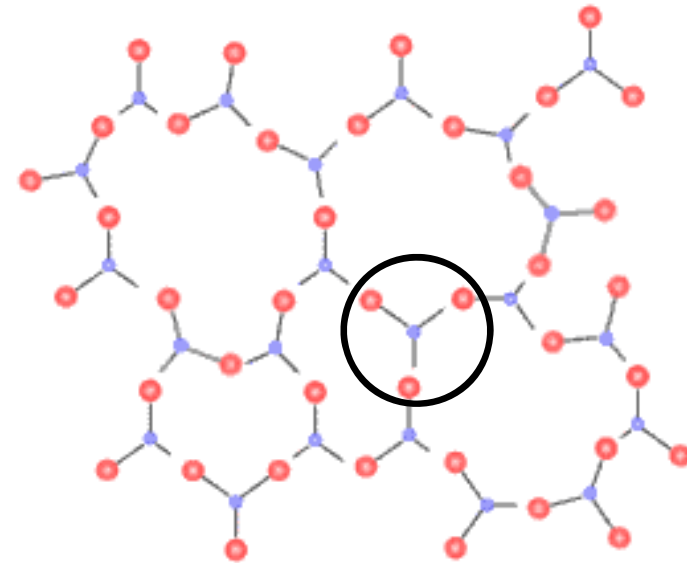
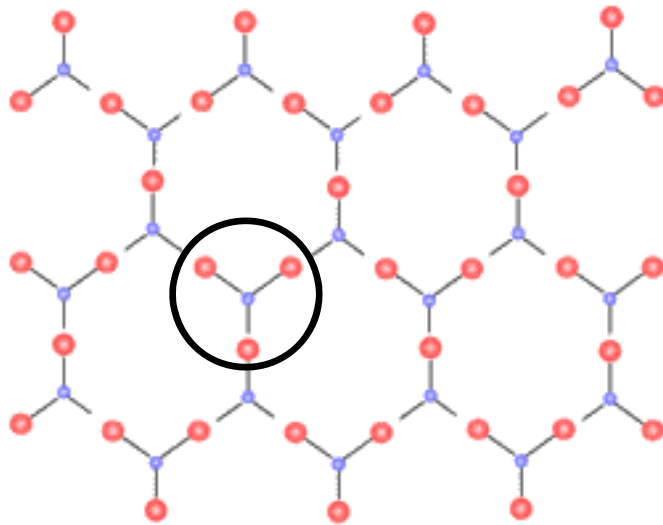
### ➤ Preporuceni prag znanja:

- Osnovne kristalografske definicije
- Kristalografska simetrija, prostorne grupe
- Difrakcija kao fizicka pojava
- Bragg-ov zakon
- Rasejanje sa jedinicne celije: strukturni faktor

# Solids

Crystalline

Amorphous



SiO<sub>2</sub> :

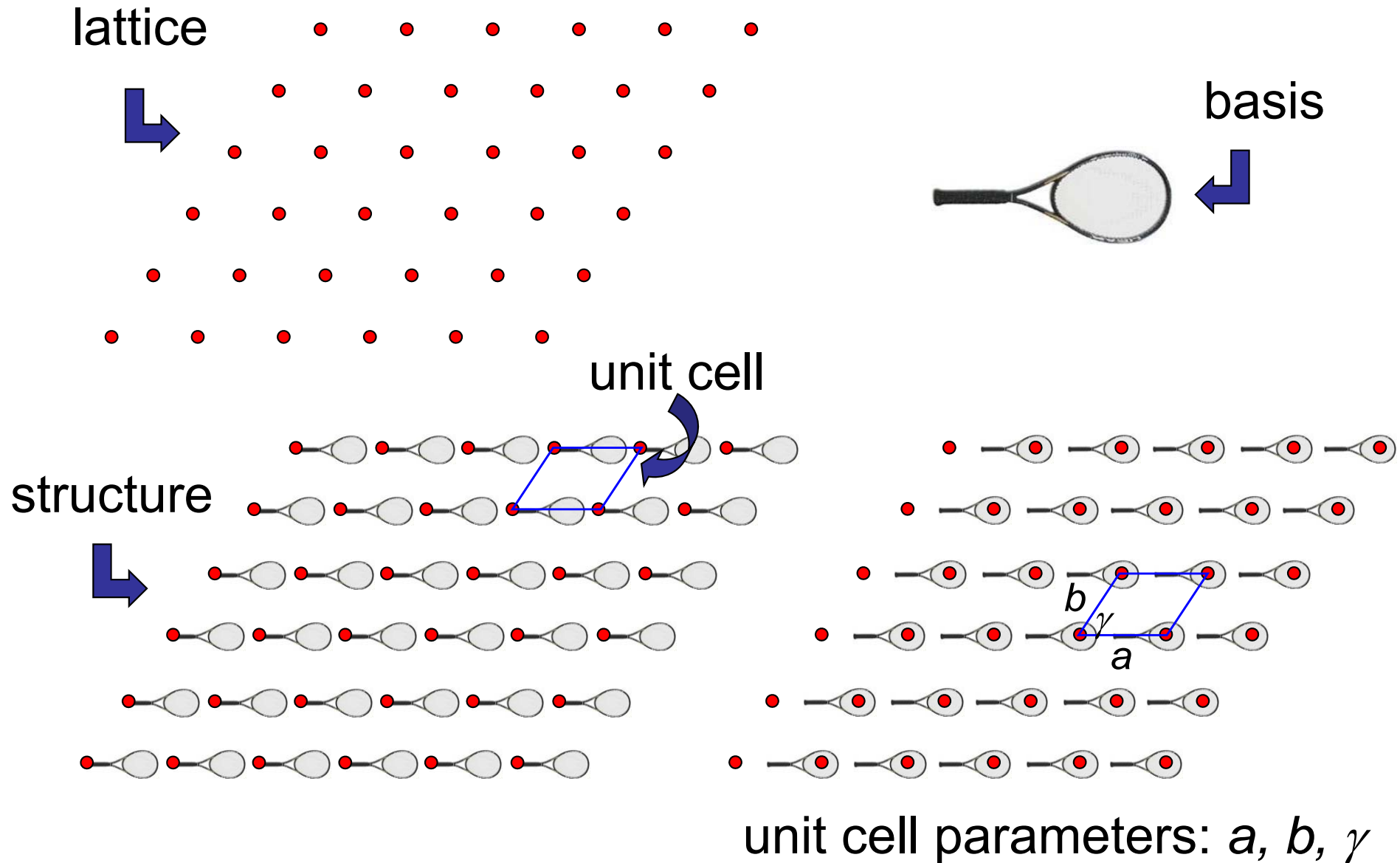
Si ●

O ●

# Crystallographic Definitions

- **Lattice** – an infinite array of points in space where each point has identical surroundings
- **Basis** – a motif associated with each lattice point
- **Crystal Structure** – the periodic arrangement of atoms in a solid
- **Unit Cell** – the smallest component from which the entire crystal can be built up, with purely translational displacements

# Crystallographic Definitions

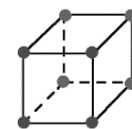


# Crystallographic Definitions

## ➤ 3D

- 14 Bravais lattices (unit cells)
- 7 crystal systems

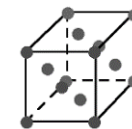
Crystal system	Lattice parameters	Min. symmetry
Cubic	$a=b=c$ $\alpha=\beta=\gamma=90^\circ$	Four $C_3$ axes
Tetragonal	$a=b \neq c$ $\alpha=\beta=\gamma=90^\circ$	$C_4$
Orthorhombic	$a \neq b \neq c$ $\alpha=\beta=\gamma=90^\circ$	Three $C_2$ axes
Rhombohedral	$a=b=c$ $\alpha=\beta=\gamma \neq 90^\circ$	$C_3$
Hexagonal	$a=b \neq c$ $\gamma=120^\circ$	$C_6$
Monoclinic	$a \neq b \neq c$ $\alpha=\gamma=90^\circ; \beta \neq 90^\circ$	$C_2$ or $m$
Triclinic	$a \neq b \neq c$ $\alpha \neq \beta \neq \gamma \neq 90^\circ$	None



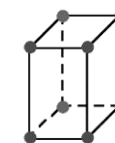
simple cubic



body-centered  
cubic



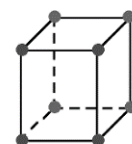
face-centered  
cubic



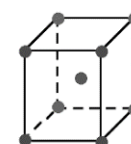
simple  
tetragonal



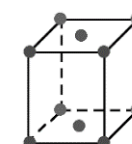
body-centered  
tetragonal



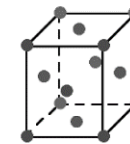
simple  
orthorhombic



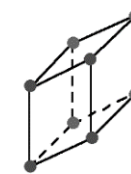
body-centered  
orthorhombic



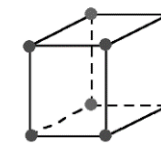
base-centered  
orthorhombic



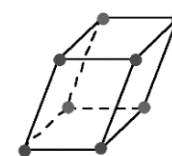
face-centered  
orthorhombic



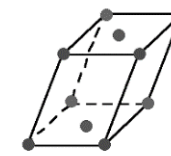
rhombohedral



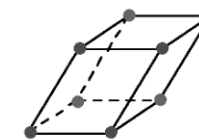
hexagonal



simple  
monoclinic



base-centered  
monoclinic



triclinic

# Symmetry in the Solid State

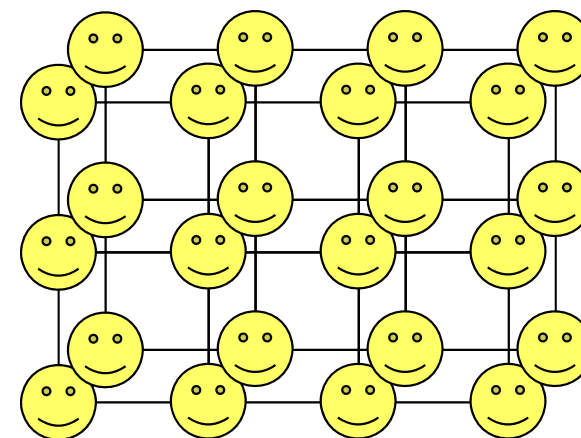
## ➤ Molecular symmetry:

- Symmetry of isolated objects
- Point group symmetry
- 32 crystallographic point groups



## ➤ Crystallographic symmetry:

- Symmetry of periodic arrays
- Space group symmetry
- 230 space groups





# Molecular Symmetry

Sym. element	Sym. operation	Symbol*
Identity	Nothing	E
Rotation axis ( $C_1, C_2, C_3, C_4, C_5, C_6 \dots$ )	Rotation	$C_n$
Inversion centre	Inversion	i
Mirror plane	Reflection	$\sigma$
Improper axis	Rotation + reflection	$S_n$

## ➤ Examples:

- Formula:  $\text{XeF}_4, \text{XeF}_2\text{Cl}_2, \dots, \text{CHFClBr}$
- Point group:  $D_{4h}, D_{2h}, \dots, C_1$

\*Schönflies notation



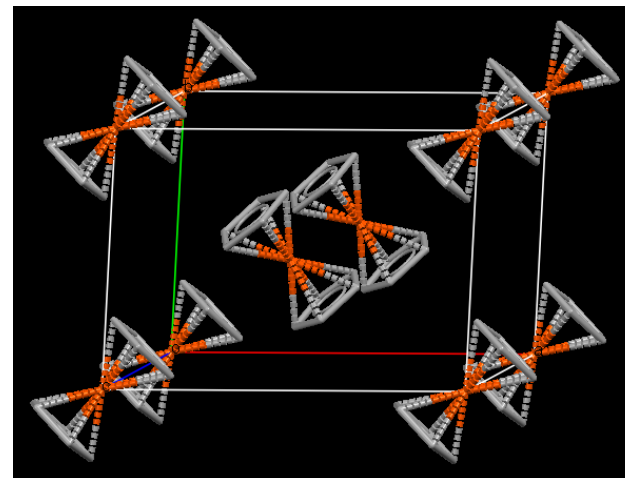
# Crystallographic Symmetry

Sym. element	Sym. operation	Symbol*
Identity	Nothing	E
Rotation axis ( $C_1, C_2, C_3, C_4, C_6$ )	Rotation	1,2,3,4,6
Inversion centre	Inversion	-1
Mirror plane	Reflection	$m$
Improper axis	Rotation + inversion	-1,-2,-3,-4,-6
Screw axis	Rotation + translation	$N_p$
Glide plane	Reflection + translation	$a, b, c, n, d$

\*Hermann-Mauguin notation

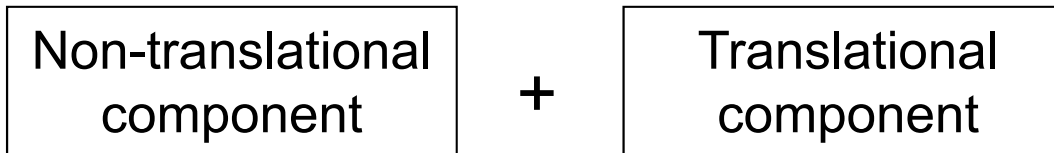
# Molecular vs. Crystallographic Symmetry

- Q: Can molecules with 5-fold symmetry form crystals?
  - Yes!
- Ferrocene (CSD refcode FEROCCE01)
  - Molecular symmetry:  $D_{5d}$
  - Space group symmetry:  $P2_1/a$



# Space Groups

- Crystal = 3D periodic array
- Full description of crystal symmetry:



## Point groups

- Take away linear
- Retain only those with 2,3,4 and 6-fold axes



- 32 crystallographic point groups

## Translations

- Unit cell translations
- Cell centring translations (F, I, C, B, A)
- Translational symmetry elements

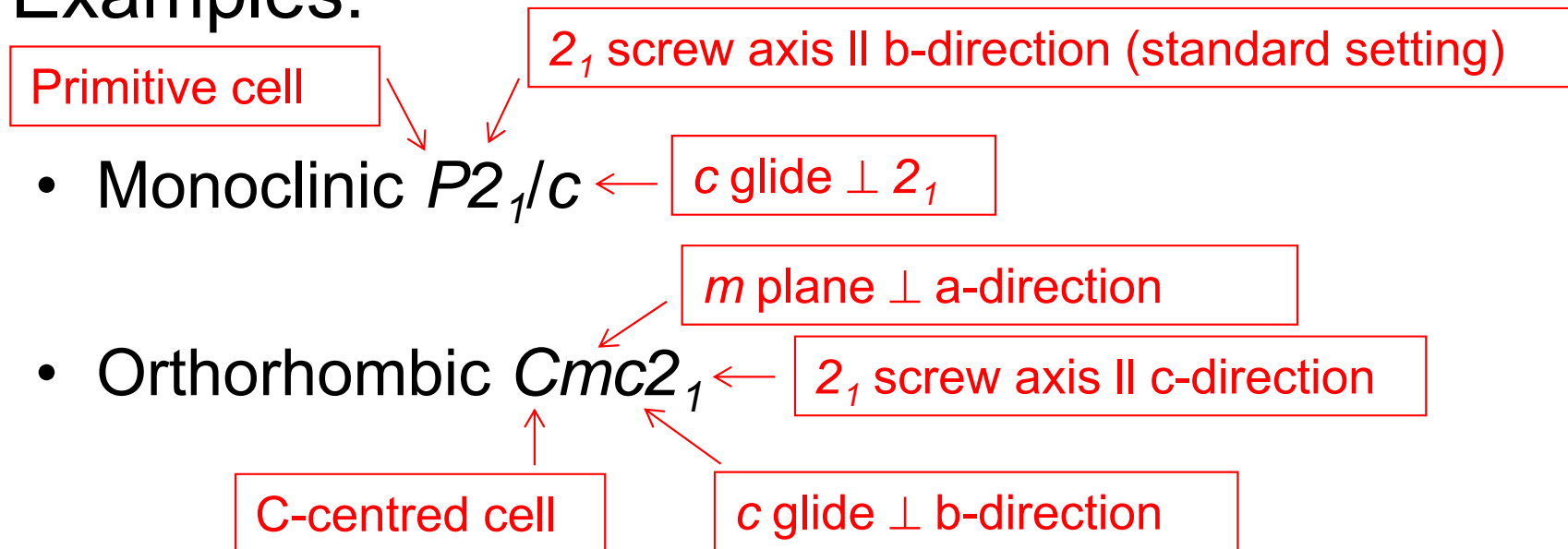


# Space Groups

## ➤ Notation:

- Condensed listing of the symmetry elements present
- First letter indicates the absence (P) or presence (I, F, A, B, C) of unit cell centring
- Space group symbol notation conventions depend on the crystal system

## ➤ Examples:



# International Tables for Crystallography

- Key information (to be able to use):
  - Short symbol
  - Crystal system
  - Positions: multiplicity, site symmetry, coordinates
  - Reflection conditions
- Other important information (to note):
  - Space group diagrams (graphical symbol list in Intro)
- Examples:  $P2_1/c$  (# 14) and  $Pnma$  (# 53)

# International Tables for Crystallography

symbol

crystal system

$P2_1/c$

$C_{2h}^5$

$2/m$

Monoclinic

CONTINUED

No. 14

$P2_1/c$

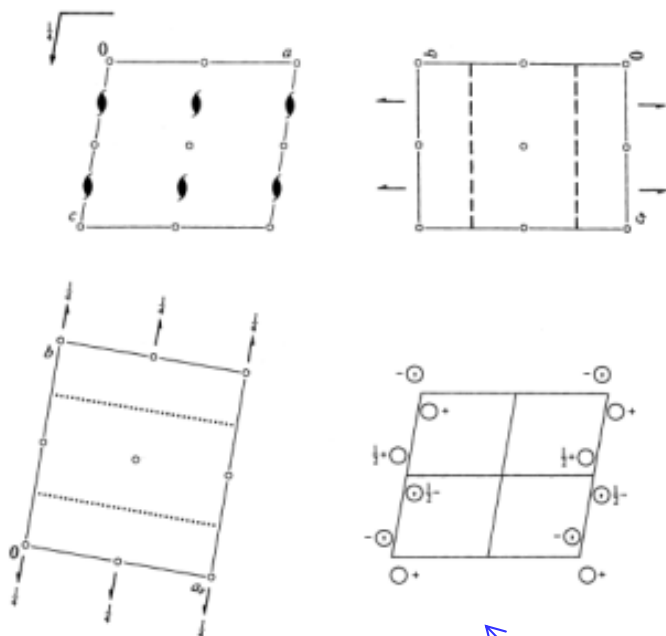
No. 14

$P12_1/c1$

Patterson symmetry  $P12_1/m1$

positions

UNIQUE AXIS  $b$ , CELL CHOICE 1



Origin at 1

Asymmetric unit  $0 \leq x \leq 1; 0 \leq y \leq \frac{1}{2}; 0 \leq z \leq 1$

Symmetry operations

(1) 1 (2)  $2(0, \frac{1}{2}, 0)$  (3)  $1(0, 0, 0)$  (4)  $c(x, \frac{1}{2}, z)$

space group diagrams  
(for illustration only!)

Generators selected (1);  $t(1, 0, 0)$ ;  $t(0, 1, 0)$ ;  $t(0, 0, 1)$ ; (2); (3)

Positions

Multiplicity,  
Wyckoff letter,  
Site symmetry

Coordinates

Multiplicity, Wyckoff letter, Site symmetry	Coordinates
4 e 1	(1) $x, y, z$ (2) $x, y + \frac{1}{2}, z + \frac{1}{2}$ (3) $x, y, z$ (4) $x, y + \frac{1}{2}, z + \frac{1}{2}$
2 d 1	$\frac{1}{2}, 0, \frac{1}{2}$ $\frac{1}{2}, \frac{1}{2}, 0$
2 c 1	$0, 0, \frac{1}{2}$ $0, \frac{1}{2}, 0$
2 b 1	$\frac{1}{2}, 0, 0$ $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$
2 a 1	$0, 0, 0$ $0, \frac{1}{2}, \frac{1}{2}$

Reflection conditions

General:

$h0l : l = 2n$   
 $0k0 : k = 2n$   
 $00l : l = 2n$

Special: as above, plus

$hkl : k + l = 2n$   
 $hkl : k + l = 2n$   
 $hkl : k + l = 2n$   
 $hkl : k + l = 2n$

Symmetry of special projections

Along [001]  $p2gm$   
 $a' = a, b' = b$   
Origin at  $0, 0, z$

Along [100]  $p2gg$   
 $a' = b, b' = c,$   
Origin at  $x, 0, 0$

Along [010]  $p2$   
 $a' = \frac{1}{2}c, b' = a$   
Origin at  $0, y, 0$

Maximal non-isomorphic subgroups

I [2] $P1c1(Pc, 7)$  1; 4  
[2] $P12_1(P2_1, 4)$  1; 2  
[2] $P1(2)$  1; 3

IIa none

IIb none

Maximal isomorphic subgroups of lowest index

IIc [2] $P12_1/c1(a' = 2a \text{ or } a' = 2a, c' = 2a + c)(P2_1/c, 14)$ ; [3] $P12_1/c1(b' = 3b)(P2_1/c, 14)$

Minimal non-isomorphic supergroups

I [2] $Pnna(52)$ ; [2] $Pmna(53)$ ; [2] $Pcca(54)$ ; [2] $Pbam(55)$ ; [2] $Pccn(56)$ ; [2] $Pbcm(57)$ ; [2] $Pnmm(58)$ ; [2] $Pbcn(60)$ ; [2] $Pbca(61)$ ; [2] $Pnma(62)$ ; [2] $Cmce(64)$   
II [2] $A12/m1(C2/m, 12)$ ; [2] $C12/c1(C2/c, 15)$ ; [2] $I12/c1(C2/c, 15)$ ; [2] $P12_1/m1(c' = \frac{1}{2}c)(P2_1/m, 11)$ ; [2] $P12_1/c1(b' = \frac{1}{2}b)(P2_1/c, 13)$

reflection conditions

# Asymmetric Unit

- The smallest portion of the structure which must be specified (coordinates) before space group symmetry defines the entire structure
- Crystallographically unique (independent) atoms
- Can be equal to/more/less than one molecule (in molecular solids)
- Can be equal to/more/less than the formula unit (in extended solids)



# Example: Benzene

## ➤ Structure details

- CSD refcode BENZEN
- Orthorhombic
- Space group *Pbca*
- Asymmetric unit: 3 C, 3 H

*Proc. R. Soc. Lond. A* 1964 **279**, 98-110

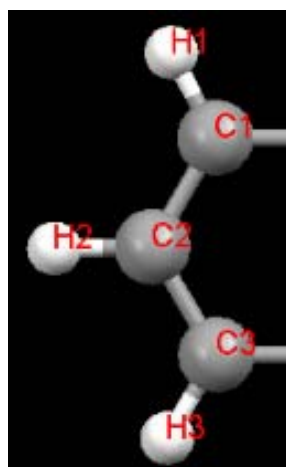
A crystallographic study of solid benzene by neutron diffraction

By G. E. BACON\*, N. A. CURRY AND S. A. WILSON

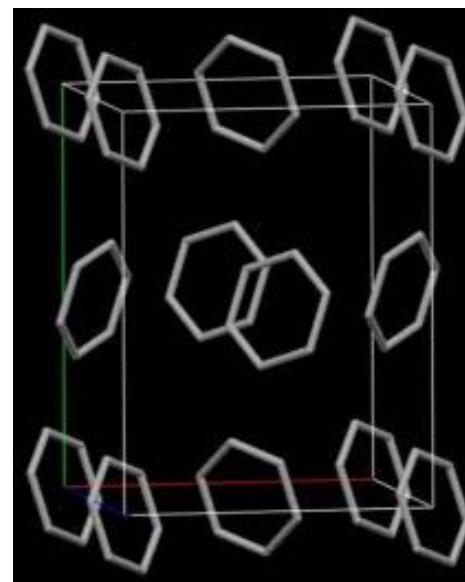
*Atomic Energy Research Establishment, Harwell*

(Communicated by R. Spence, F.R.S.—Received 17 September 1963—Read 6 February 1964)

A study by neutron diffraction of crystals of solid benzene at  $-55$  and  $-135$  °C has extended the earlier picture of the molecular structure provided by Cox's X-ray work at  $-3$  °C. Neutron reflexions in four crystal zones have been examined, leading to values of the atomic co-ordinates and thermal parameters. Superimposed upon the random motion of the carbon



*Pbca*  
→  
symmetry



# Diffraction by Crystalline Solids

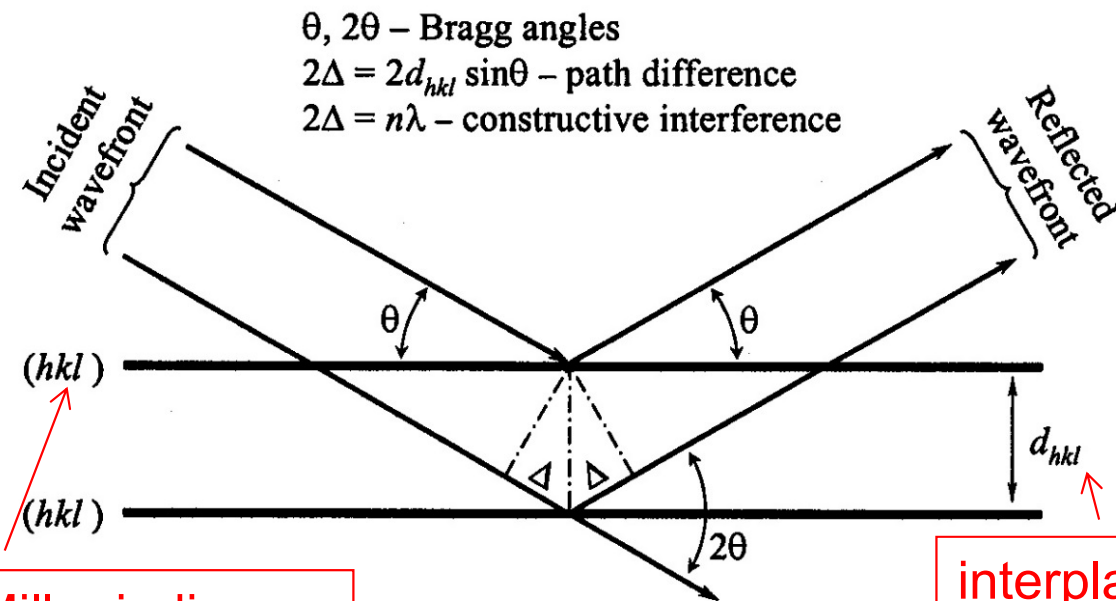
- Crystalline materials = long-range 3D periodic atomic arrays
  - Interatomic distances  $\sim 0.5 - 2.5 \text{ \AA}$
- Waves of comparable wavelengths will be diffracted
  - X-rays = EM radiation,  $\lambda \sim 0.1 - 100 \text{ \AA}$
  - Neutrons
  - Electrons
$$\left. \begin{array}{l} \text{Neutrons} \\ \text{Electrons} \end{array} \right\} \lambda = h / mv$$

⇓
- X-rays, neutrons and electrons are diffracted by crystals

⇓
- X-ray, neutron and electron diffraction patterns contain information about 3D arrangement of atoms in crystals

# Bragg's Law

- Simplistic, but useful view of diffraction
  - Atoms arranged in parallel planes in a crystal
  - Incident X-rays reflected off the planes
  - Peaks in diffraction patterns referred to as “reflections”



$$2\Delta = n\lambda$$

( $n$ =order of diffraction\*)

$$2d_{hkl} \sin\theta = \lambda$$


Miller indices

interplanar spacing,  
d-spacing

\* $n=1$ , because  $n^{\text{th}}$  order diffraction from  $(hkl)$  planes with spacing  $d$  can be treated as 1<sup>st</sup> order diffraction from  $(nh, nk, nl)$  planes with spacing  $d/n$

# Structure Factor

- Peak intensities,  $I_{hkl}$ :  $I_{hkl} \propto |F_{hkl}|^2$
- $|F_{hkl}| \sim$  the collective scattering power of the atoms in the unit cell
  - Other factors: absorption, thermal vibrations, site occupancies, ...
- Structure factor,  $F_{hkl}$

$$F_{hkl} = \sum_1^N f_n e^{2\pi i(hx_n + ky_n + lz_n)}$$


Electronic property of the atom  
Information about atom types

Structural property of the unit cell  
Information about atomic positions

\* $x_n$ ,  $y_n$  and  $z_n$  are atomic fractional coordinates:  $x_n = x/a$ ,  $y_n = y/b$ ,  $z_n = z/c$